

EE 411 Homework 1 Solutions

1)

a-)

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octave:1> c=68e-12;
octave:2> l=400e-9;
octave:3> r=5e3;
octave:4> fres=(1/sqrt(l*c))/(2*pi)
fres = 3.0517e+07 = 30.517 MHz
```

b-)

i. At resonance impedance of the inductor is equal to $R_p = 5K$

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ii. octave:10> imp_c=1/(j*2*pi*fres*0.5*c)
imp_c = 0.00000 - 153.39300i
octave:11> imp_l=j*2*pi*fres*0.5*l
imp_l = 0.00000 + 38.34825i
octave:12> 1/(power(imp_c,-1)+power(imp_l,-1)+power(5000,-1))
ans = 0.52282 + 51.12565i
```

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iii. octave:14> imp_c=1/(j*2*pi*fres*2*c)
imp_c = 0.00000 - 38.34825i
octave:15> imp_l=j*2*pi*fres*2*l
imp_l = 0.00000 + 153.39300i
octave:16> 1/(power(imp_c,-1)+power(imp_l,-1)+power(5000,-1))
ans = 0.52282 - 51.12565i
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iv. octave:23> imp=0.52282 + 51.12565i
imp = 0.52282 + 51.12565i
octave:24> eff_inductance=imag(imp)/(2*pi*fres*0.5)
eff_inductance = 5.3328e-07 = 533.28 nH at @ f_resonance/2
octave:25> imp=0.52282-j*51.12565
imp = 0.52282 - 51.12565i
octave:26> eff_inductance=imag(imp)/(2*pi*fres*2)
eff_inductance = -1.3332e-07 = -133 nH @ 2*f_resonance
```

Negative inductance is rather meaningless calculating the effective capacitance

$$\text{eff_cap} = 1 / (2 * \pi * 2 * \text{fres} * \text{abs}(\text{imag}(\text{imp})))$$

$\text{eff_cap} = 5.1005\text{e-}11 = \mathbf{50 \text{ pF}}$ at twice the resonance frequency the inductor acts as a capacitor.

2)

a-)

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octave:1> c=2e-9;
octave:2> l=0.7e-9;
octave:3> r=25e-3;
octave:4> fres=(1/sqrt(l*c))/(2*pi)
fres = 1.3451e+08 = 134.51 MHz
```

b-)

i. at resonance the impedance of the capacitor is equal to 25 mΩ

ii. octave:5> $\text{imp_l} = j * 2 * \pi * \text{fres} * 0.5 * l$

$\text{imp_l} = 0.00000 + 0.29580i$

octave:6> $\text{imp_c} = 1 / (j * 2 * \pi * \text{fres} * 0.5 * c)$

$\text{imp_c} = 0.00000 - 1.18322i$

octave:7> $\text{imp} = \text{imp_c} + \text{imp_l} + r$

$\text{imp} = 0.025000 - 0.887412i$

iii. octave:8> $\text{imp_c} = 1 / (j * 2 * \pi * \text{fres} * 2 * c)$

$\text{imp_c} = 0.00000 - 0.29580i$

octave:9> $\text{imp_l} = j * 2 * \pi * \text{fres} * 2 * l$

$\text{imp_l} = 0.00000 + 1.18322i$

octave:10> $\text{imp} = \text{imp_c} + \text{imp_l} + r$

$\text{imp} = 0.025000 + 0.887412i$

iv. octave:11> $\text{eff_inductance} = \text{imag}(\text{imp}) / (2 * \pi * \text{fres} * 2)$

$\text{eff_inductance} = 5.2500\text{e-}10 = \mathbf{0.525 \text{ nH @ } 2 * \text{fres}}$

octave:22> $\text{imp} = 0.025 - j * 0.887412$

$\text{imp} = 0.025000 - 0.887412i$

octave:23> $1 / (2 * \pi * \text{fres} * 0.5 * \text{abs}(\text{imag}(\text{imp})))$

$\text{ans} = 2.6667\text{e-}09 = \mathbf{2.66 \text{ nF @ } \text{fres} / 2}$