

**Question 1 (15 points):**

- a) (7 points) Match  $R_L = 50 \Omega$  into  $R_{in} = 5 \Omega$  with  $Q = 6$  by using a T-match circuit and find the impedances of the components. Draw the circuit for low-pass response.
- b) (8 points) Match  $R_L = 50 - j20 \Omega$  into  $R_{in} = 5 \Omega$  with  $Q = 6$  again by using a T-match circuit and find the impedances of the components. You can use a high-pass or low-pass circuit as required.

a-)  $R_L = 50 \Omega$   
 $R_{in} = 5 \Omega = K = 10$

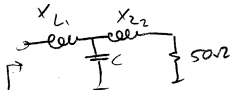
$$Q_L = \frac{[Q^2 K + 2K - K^2 - 1]^{1/2} - Q}{K - 1}$$

$$= \frac{[36 \times 10 + 20 - 100 - 1]^{1/2} - 6}{9} = \frac{(360 + 20 - 100 - 1)^{1/2} - 6}{9}$$

$$= \frac{279^{1/2} - 6}{9} = 1.19 \Rightarrow |X_{L2}| = Q_L \times 50 = 1.19 \times 50 = 59.5 \Omega$$

$Q_L = 6 - 1.19 = 4.81$

$Q_R = \frac{X_{L2}}{50 \Omega} \Rightarrow$



$X_{L2} = 1.19 \times 50 = 59.5 \Omega$

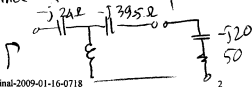
$R_{in} = 5 \Omega$

$Q_L = \frac{X_{L1}}{R_{in}} \Rightarrow X_{L1} = 4.81 \times 5 = 24.05 \Omega$

$R_p = (Q^2 + 1) 50 \Omega = 120.805$

$Q_T = 6 = \frac{R_p}{X_C} = \frac{120.805}{X_C} \Rightarrow |X_C| = \frac{120.805}{6} = 20.13 \Omega$

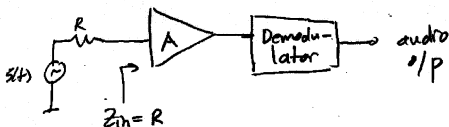
b-) Since the reactive part is negative, the configuration becomes



$$(-) (F_2 k T_0 B)_{dB} = IP3 = IIP3 - 3(IIP3 - S_{in}) = 3S_{in} - 2IIP3$$

$$(F_2 k T_0 B)_{dB} + 2IIP3 = 3S_{in} = \frac{-126.8 + 2 \times 20}{3} = -28.9 \text{ dBm}$$

Question 2 (25 points):



The circuit shown above is constructed with an amplifier with  $G=9\text{dB}$ ,  $F=4\text{dB}$  and  $IIP3=20\text{dBm}$ . The noise figure of the demodulator is  $10\text{dB}$ . The amplifier presents matched load to the source. The noise bandwidth of the modulator is  $50\text{ kHz}$  and it requires at least  $12\text{ dB S/N}$  at its input to function properly.

- (10 points) What is the noise temperature of the system, \_\_\_\_\_ in dBm
- (5 points) Find the signal level  $s(t)$  to let the demodulator function properly,
- (10 points) If there are two equal-amplitude unwanted interfering signals at the input such that their third-order intermodulation product falls into the receiver bandwidth, what is the signal level which decreases the S/N at the input of the demodulator by  $3\text{dB}$ ?

a-)  $G = 8 \text{ times}$ ,  $F_1 = 2.51 \text{ times}$ ,  $F_2 = 10 \text{ times}$

$$F_{1,2} = 2.5 + \frac{10-1}{8} = 2.5 + \frac{9}{8} = 3.625$$

$$T = (F+1) 300 \text{ K} = (3.625-1) \times 300 = 787.5 \text{ K}$$

b-)  $* k T B F \left( \frac{S}{N} \right) = 1.38 \times 10^{-23} \times 300 \times 50 \times 10^3 \times 16$   
 $= 3.312 \times 10^{-15} \text{ W} = 3.312 \times 10^{-12} \text{ dB mWatts}$   
 $= -114.8 \text{ dBm}$

c-)  $-114.8 \text{ dBm}$  is  $12 \text{ dB}$  above noise level  $\Rightarrow$   
 noise level  $= -114.8 + 12 = -126.8 \text{ dBm}$   
 to increase noise + interference by  $3 \text{ dB} \Rightarrow$   
 interference level  $= -126.8 \text{ dBm} = \text{level of 3rd order int-products referred to the input.}$

$$20 - \frac{(20 - (-126.8))}{3} = \text{int. signal level} = -28.93 \text{ dBm}$$

$$\approx -29 \text{ dBm}$$

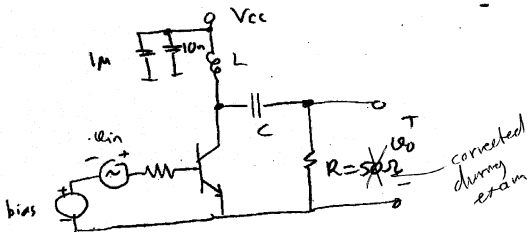
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b-)  $* k T_0 B = 2 \times 10^{-16} \text{ Watts} = 3 \text{ dB} - 160 \text{ dB} = -157 \text{ dB dBW} = -127 \text{ dBm}$   
 $F_2 k T_0 B = 3.65 \times 2 \times 10^{-16} = 7.3 \times 10^{-16} \text{ W} = -151.2 \text{ dBW} = -121.2 \text{ dBm}$

**Question 3 (20 points):**



A power amplifier as shown above is operated at 100 MHz. It is driven to function in class-B mode. The transistor  $T_1$  can handle 2A and 20V as maximum current and voltage respectively without being damaged.

- (10 points) Find the values of  $V_{cc}$ ,  $C$  and  $L$  in order to get the maximum power output from this amplifier,
- (5 points) Find the maximum output power,
- (5 points) Find the average current drawn from the power supply at the maximum output level.

$$a-) R = \frac{V_{max}}{I_{max}} = \frac{20V}{2A} = 10\Omega \Rightarrow \text{Match } 5\Omega \text{ into } 10\Omega$$

$$\frac{10\Omega}{2} = 5\Omega \quad 1+Q^2 = 1+1^2 \Rightarrow Q=1$$

$$|X_C| = Q \times R_L = 5\Omega \Rightarrow C = \frac{1}{\omega X_C} = 3.18 \times 10^{-9} F = 3.18 pF$$

$$Q = \frac{R}{|X_L|} = \frac{10}{|X_L|} \Rightarrow |X_L| = \frac{10}{1} = 10\Omega$$

$$V_{cc} = \frac{V_{max}}{2} = 10V$$

$$L = \frac{X_L}{\omega} = 6.39 \times 10^{-8} H = 15.9 nH$$

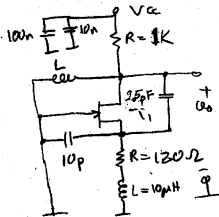
$$b-) P_{out} = \frac{V_P}{2} \times \frac{I_P}{2} = \frac{10V \times 1A}{2} = 5W$$

$$c-) I_{av} = \frac{1}{T} \int_0^T i(t) dt =$$

$$\text{or } \frac{10V}{\sqrt{2}} \times \frac{\sqrt{2}A}{2} = 5W$$

$$= \frac{1}{T} \int_0^{T/2} I_{RF} \sin \frac{2\pi}{T} t dt = \frac{I_{RF}}{\pi} = \frac{2A}{\pi} = 0.636 A$$

**Question 4 (20 points) :**



$L = 10\mu H$  is too large  
sinavda söylendi.

An oscillator as shown above is constructed. Please answer the following:

- (7 points) Find the minimum transconductance of the transistor to start the oscillation,
- (6 points) Find the value of  $L$  to have the oscillation at 70 MHz,
- (7 points) Find the source current of the transistor  $T1$  in order to have 2Vp-p output voltage

$$a-) g_m > \frac{1}{R_n(1-n)} = \frac{1}{1000 \cdot 0.2 \cdot 0.8} = 0.00625 \text{ mhos}$$

$$b-) C_{eq} = \frac{10 \times 2.5}{12.5} = 2 \text{ pF} \quad L = \frac{1}{\omega^2 C} = \frac{1}{(2\pi \cdot 70 \times 10^6)^2 \cdot 2 \times 10^{-12}} = 2.58 \times 10^{-6} = 2.58 \mu H$$

$$c-) V_{tan/c} = V_p = 2 I_{BIAS} R(1-n)$$

$$I_{BIAS} = \frac{1}{2 \times 1000 \times 0.8} = 6.25 \times 10^{-4} A = 0.625 \text{ mA}$$

$$10 \mu\text{H} \rightarrow X_L = 10 \times 10^{-6} \times \omega = 4.398 \text{ K} \approx 4.4 \text{ K} = X_{L_s}$$

$$R_s = 120 \Omega \quad \rightarrow Q = \frac{4400}{120} = 36.65$$

$$R_p = (Q^2 + 1) R_s = 1344 \times 120 = 161323 \Omega$$

$$X_p = \frac{4.4 \times 1344}{1.25} \approx 4.4 \text{ K}$$

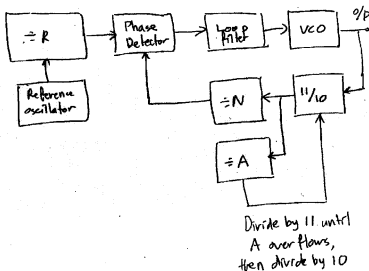
$$L_p \approx 10 \mu\text{H}$$

$\Rightarrow R_p$  is negligible even before it is divided by  $n^2$

$$R_p \text{ over the tank} = \frac{161323 \Omega}{0.2^2} = 4 \text{ M}\Omega$$

$$\frac{L_p}{n^2} = \frac{10 \mu\text{H}}{0.2^2} = 10 \mu\text{H} \times 25 = 250 \mu\text{H}$$

**Question 5 (20 points) :**



The block diagram of a PLL circuit is given above. The reference oscillator frequency is 10 MHz. The operating frequency range of the PLL is 500-600 MHz. The channel spacing is 100kHz. Maximum possible phase detector frequency is used in the system.

- (5 points) Find the value of R,
- (10 points) Find the minimum value of the register A and the <sup>minimum</sup> maximum value of the register N in order to be able to generate all the frequencies in the range given above.
- (5 points) Find a set of values of N and A for generating an output frequency of 555.5 MHz within the constraints of step (b).

$$a-) R = 100 = \frac{10 \text{ MHz}}{0.1 \text{ MHz}}$$

b-)  $M = NP + A$  where  $P=10$  and  $A < N$   
 $A_{\min} = 9$  is needed to cover the intermediate frequencies when  $N$  is increased by one.  
 $M$  for 100 MHz is 6000  
 $6000 = N \times 10 + 0 \Rightarrow N = \frac{6000}{10} = 600$

c-)  $555.5 = NP + A \Rightarrow A = 5, N = 555$