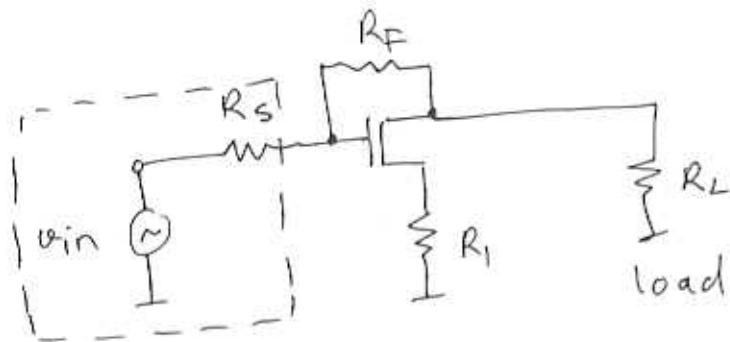


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(1)

## The Shunt-Series Amplifier

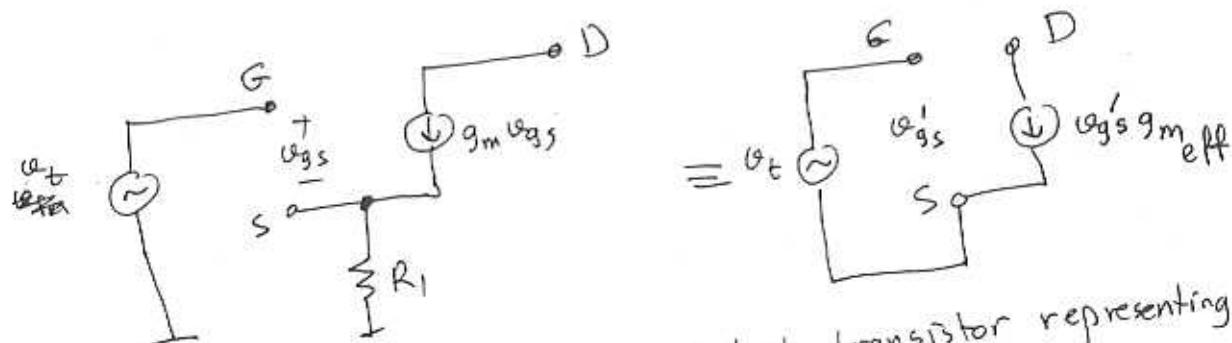


Source

This is an amplifier which has controlled gain and input and output impedances. At low enough frequencies and if the effect of  $R_F$  is neglected then

$$A_v \approx -\frac{R_L}{R_1} \quad (\text{open-loop gain})$$

But for a more precise calculation of the gain, let us first find the equivalent circuit for the source degeneration.



Can we define an equivalent transistor representing the  $R_1$  and transistor combination.

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 (2)

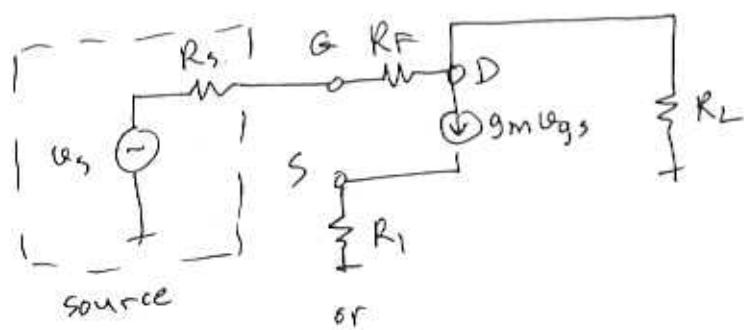
$$\vartheta_{gs} = \vartheta_t - \vartheta_s = \vartheta_t - g_m u_{gs} R_i$$

$$\Rightarrow u_{gs}(1 + g_m R_i) = \vartheta_t \Rightarrow i_o = g_m u_{gs} = \vartheta_t \frac{g_m}{1 + g_m R_i}$$

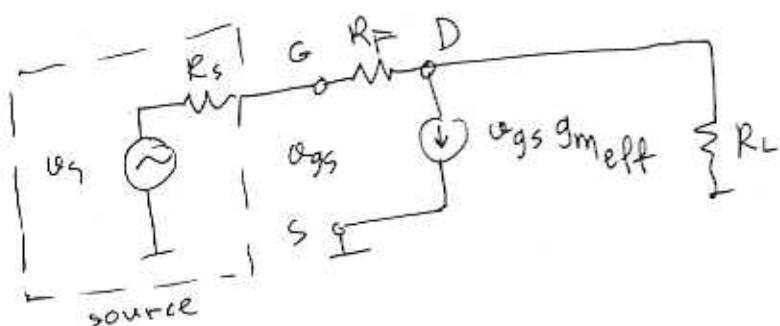
Therefore we can replace the transistor with an source degeneration resistor  $R_i$  by another transistor with transconductance equal to

$$\boxed{\frac{g_m}{g_m R_i + 1} = g_{m\text{eff}}}$$

The <sup>small signal</sup> equivalent circuit of the shunt-series amplifier is:



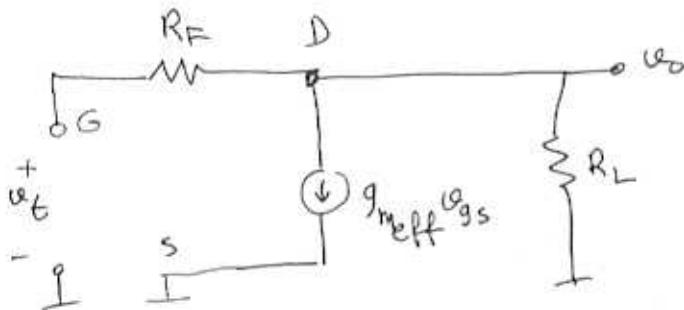
or



$$\text{where } g_{m\text{eff}} = \frac{g_m}{1 + g_m R_i}$$

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 (3)

If we define the gain of the amplifier as  $\frac{v_o}{v_g}$ ,  
 then we can draw the equivalent circuit as:



By superposition

$$v_o = v_t \underbrace{\frac{R_L}{R_F + R_L}}_{\text{load current contribution from the current source}} - v_t g_{\text{meff}} \cdot \underbrace{\frac{R_F}{R_F + R_L} \cdot R_L}_{\text{load current contribution from the feedback resistor}}$$

$$A_v = \frac{v_o}{v_t} = \frac{R_L}{R_F + R_L} \left[ 1 - \underbrace{\frac{g_m}{1 + g_m R_i} \cdot R_F}_{g_{\text{meff}}} \right]$$

If we continue rearranging  $A_v$  as below:  
 to express  $A_v$  in terms of  $-\frac{R_L}{R_i}$  times  
 modifying factors

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 (4) (20-10-2005)

$$\begin{aligned}
 A_v &= \frac{R_L}{R_F + R_L} \left[ 1 - \frac{g_m}{1+g_m R_i} R_F \right] \\
 &= -\frac{R_L}{R_F + R_L} \left[ \frac{g_m R_F - 1 - g_m R_i}{1+g_m R_i} \right] \\
 &= -\frac{R_L}{R_i} \cdot \left[ \frac{g_m R_F - 1 - g_m R_i}{g_m + \frac{1}{R_i}} \right] \cdot \frac{1}{R_F + R_L} \\
 &= -\frac{R_L}{R_i} \left[ \frac{R_F - \frac{1}{g_m} - R_i}{1 + \frac{1}{g_m R_i}} \right] \frac{1}{R_F \left( 1 + \frac{R_L}{R_F} \right)} \\
 &= -\frac{R_L}{R_i} \cdot \frac{1}{1 + \frac{1}{g_m R_i}} \cdot \frac{1}{1 + \frac{R_L}{R_F}} \left[ 1 - \frac{1}{g_m R_F} - \frac{R_i}{R_F} \right] \\
 &= -\frac{R_L}{R_i} \frac{1}{1 + \frac{1}{g_m R_i}} \cdot \frac{1}{1 + \frac{R_L}{R_F}} \left[ 1 - \frac{1 + R_i g_m}{g_m R_F} \right] \\
 &= -\frac{R_L}{R_i} \left[ \frac{1}{1 + \frac{1}{g_m R_i}} \right] \cdot \left[ \frac{1}{1 + \frac{R_L}{R_F}} \right] \left[ 1 - \frac{1}{g_{meff} R_F} \right]
 \end{aligned}$$

all of the expressions inside the parentheses  
 are less than one. If  $\frac{1}{g_m R}$ ,  $\frac{R_L}{R_F}$

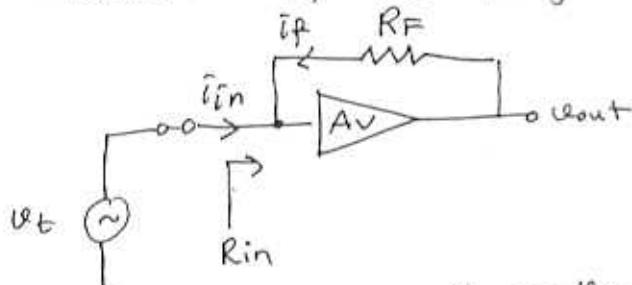
and  $\frac{1}{g_{meff} R_L}$  are much less than one,

then the gain approaches  $-\frac{R_L}{R_i}$

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(5)

In order to calculate the i/p impedance of the shunt-series amplifier, we can make use of the formula giving the input impedance of the  $h\infty$  input impedance amplifier with the feedback resistance  $R_F$  and the gain  $A_v$ .



$$i_{in} = -i_f = -\frac{v_{out} - v_t}{R_F} = -\frac{v_t A_v - v_t}{R_F} = v_t \frac{(1 - A_v)}{R_F}$$

$$\Rightarrow R_{in} = \frac{v_t}{i_{in}} = \frac{R_F}{1 - A_v}$$

Substituting the expression for  $A_v$  into the eqn. above:

$$R_{in} = \frac{R_F}{1 - \frac{R_L}{R_F + R_L} \left[ 1 - R_F g_{m_{eff}} \right]} \quad \text{letting } R_E = \frac{1}{g_{m_{eff}}}$$

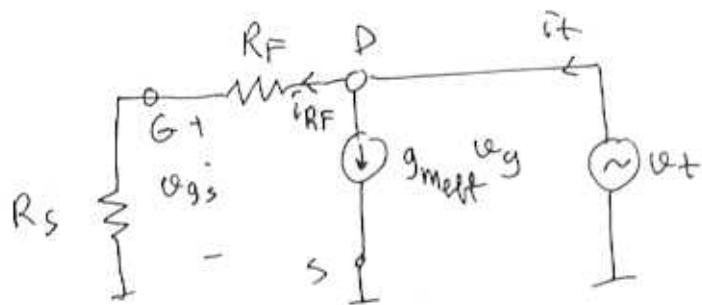
$$\begin{aligned} R_{in} &= \frac{R_F}{1 + \frac{R_L}{R_F + R_L} \left[ \frac{R_F}{R_E} - 1 \right]} = \frac{R_F}{1 + \frac{R_L [R_F - R_E]}{R_E [R_F + R_L]}} \\ &= \frac{R_F R_E [R_F + R_L]}{R_E [R_F + R_L] + R_L [R_F - R_E]} = \frac{R_F \cdot R_E [R_F + R_L]}{R_E R_F + R_E R_L + R_L R_F - R_L R_E} \end{aligned}$$

$$R_{in} = \frac{R_F \cdot R_E [R_F + R_L]}{R_F [R_E + R_L]} = R_E \frac{[R_F + R_L]}{R_E + R_L}$$

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(6)

In order to find the o/p impedance of the shunt-series amplifier, we connect a test source to the output



By adding  $i_{RF}$  and the current source

$$i_t = \frac{v_t}{R_F + R_S} + g_{m\text{eff}} v_t \frac{R_S}{R_S + R_F} = v_t \cdot \frac{1}{R_S + R_F} [1 + R_S g_{m\text{eff}}]$$

$$= v_t \frac{1 + g_{m\text{eff}} R_S}{R_S + R_F} \Rightarrow$$

$$\frac{v_E}{i_t} = \frac{R_S + R_F}{1 + \frac{R_S}{R_E}} \quad \text{by } R_E = \frac{1}{g_{m\text{eff}}}$$

$$= R_E \frac{R_S + R_F}{R_E + R_S}$$

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$$R_{in} = R_E \frac{R_F + R_L}{R_E + R_L} \quad \text{and} \quad R_{out} = R_E \frac{R_F + R_S}{R_E + R_S}$$

If  $R_S$  is chosen as equal to  $R_L$ , then  $R_{in}$  becomes equal to  $R_D$  and

$$R_{in} = R_{out} = R_E \frac{R_F + R}{R_E + R} \quad \text{where } R_S = R_L = R$$

For designing a shunt-series amplifier the following equations are useful:

If we would like to have  $R = R_S = R_L$ , then:

$$R = R_E \frac{R_F + R}{R_E + R} \Rightarrow R R_E + R^2 = R_E (R_F + R)$$

$$\Rightarrow R_E (R_F + R - R') = R^2 \Rightarrow R_E = \frac{R^2}{R_F}$$

$$R_E = \frac{R^2}{R(1-A_v)} = \frac{R}{1-A_v} \quad \text{and} \quad R = \frac{R_F}{1-A_v}$$

and

$$R_E = \frac{g_m R_i + 1}{g_m} \Rightarrow R_E g_m = g_m R_i + 1$$

$$\Rightarrow R_i = \frac{g_m R_E - 1}{g_m} = R_E - \frac{1}{g_m}$$

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7-A

Explanation of equal input & output impedances  
at a shunt-series amplifier.

$$R_{in} = R_E \frac{R_F + R_L}{R_E + R_L} = R_o = R_E \frac{R_F + R_S}{R_E + R_S} = R = R_L = R_S$$

is there a such solution?

$$R = R_E \frac{R_F + R}{R_E + R} = R_E \frac{R_F + R}{R_E + R}$$

Obviously the quotients are equal. The only requirement is to find pairs of  $R_E$  &  $R_F$  to satisfy the condition on the left.

$$R_E + R^2 = R_E R_F + R_E R \Rightarrow \boxed{R_E R_F = R^2}$$

is the condition defining the pairs of  $R_E$  &  $R_F$ .

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(8)

Design example: (Shunt-series amp)

Design an amplifier with input & output impedances equal to  $600\Omega$ . The gain of the amplifier when driven by a  $600\Omega$  source and being loaded by  $600\Omega$  ohms must be 10 dB. The transconductance of the transistor to be used is  $12mS$ .

$$10\text{db} \rightarrow A_v = -10^{\frac{1}{2}} = -3.1622$$

$$R_i = R_E - \frac{1}{g_m} = \frac{600}{1-A_v} - \frac{1}{g_m} = \frac{600}{4.1622} - \frac{1}{12 \times 10^3}$$

$$= 144.1518 - 83.33 = 60.818\Omega$$

$$R_i = R_E - \frac{1}{g_m} = 60.818\Omega$$

Here  $R_i$  must be a positive reasonable resistor. Therefore from this equation, it can be seen if the values of  $R$ ,  $A_v$  and  $g_m$  are compatible or not.

As the last step  $R_f$  can be found from

$$R_f = R(1-A_v) = 2497.32\Omega$$

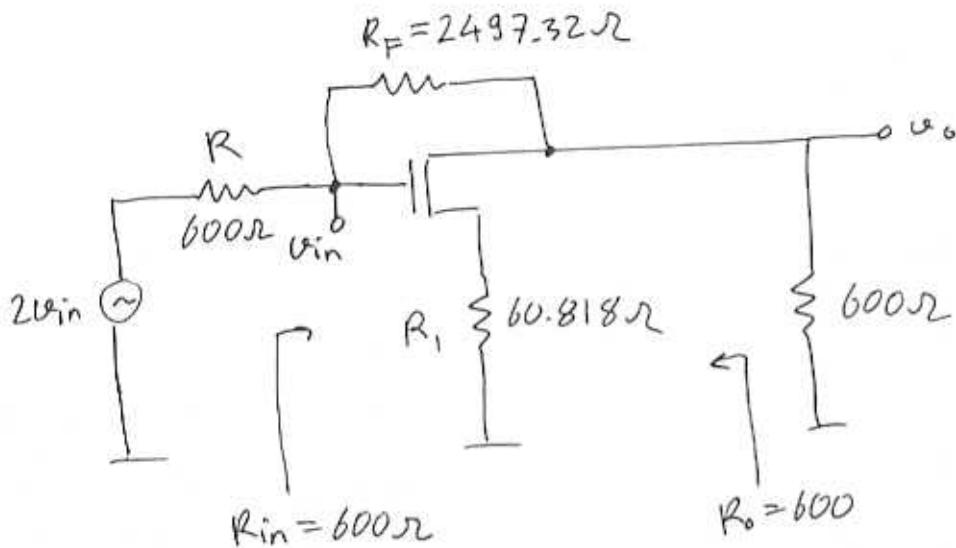
as a check  $R_i$  can be calculated from

$$R_E = \frac{R}{1-A_v} = 144.1545 \text{ (a slight calculation error)}$$

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(9)

The amplifier becomes:



$$\frac{v_o}{v_{in}} = -3.1622 \Rightarrow 10 \text{ dB}$$

$$R_E = \frac{g_m R_1 + 1}{g_m} = 144.1518\Omega$$

$$R_{in} = R_E \frac{R_F + R}{R_E + R} = 144.1518 \frac{2497.32 + 600}{144.1518 + 600} = 600\Omega$$

$$R_{out} = R_{in}$$

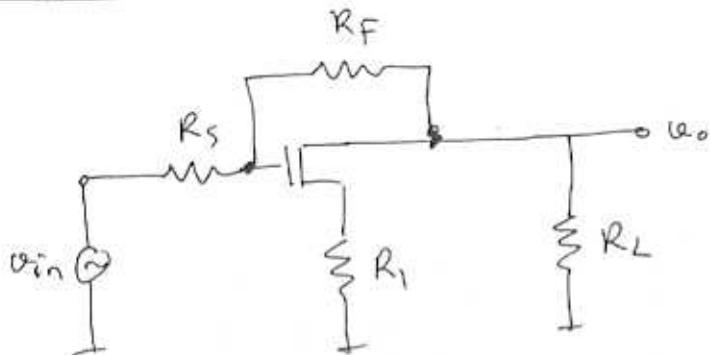
$$A_v = + \frac{R}{R_F + R} \left[ 1 - \frac{R_F}{R_E} \right] = -3.1622$$

$$g_m R_1 = 0.72 \quad A_v = 3.16$$

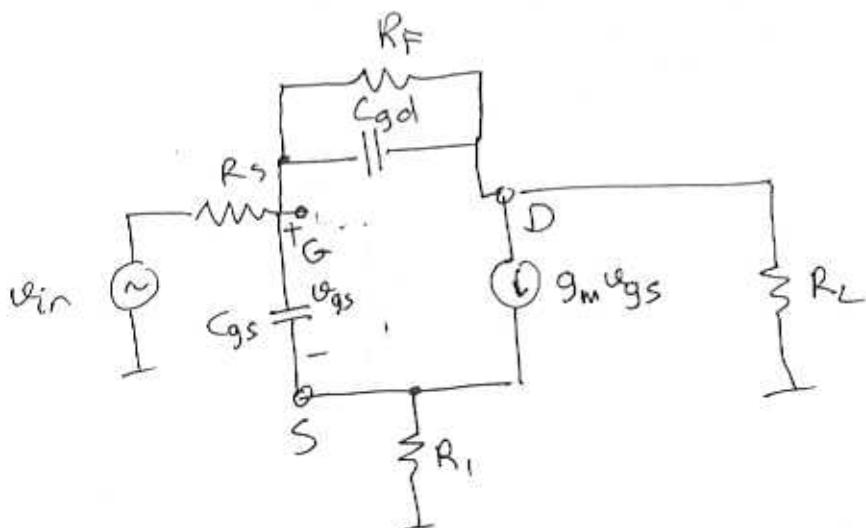
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①

Bandwidth, input-output impedances  
as a function of frequency



The high frequency equivalent circuit of the shunt-series amplifier, if  $C_{gs}$ ,  $C_{gd}$  and  $g_m$  only taken into the model, becomes:



Since this is a low order system,  $\Rightarrow$  open circuit time constants is a good estimate of the BW.  
Assume  $R_s = R_L = R$  as it is the usual application.

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(2)

The resistance facing  $C_{gd}$  is

$$R_{gd} = R_F // R_{eq} \text{ where}$$

$$R_{eq} = r_{left} + r_{right} + g_{m\text{eff}} r_{left} r_{right} \text{ where } g_{m\text{eff}} = \frac{g_m}{1+R_1 g_m}$$

$$R_{eq} = R + R + g_{m\text{eff}} R^2 \Rightarrow$$

$$R_{gd} = R_F // R \left[ 2 + g_{m\text{eff}} R \right]$$

$$\text{but } R_F = R_{in} (1 - A_v) = R(1 - A_v)$$

$$\Rightarrow R_{gd} = R(1 - A_v) // R \left[ 2 + R g_{m\text{eff}} \right]$$

$$= R \left[ (1 - A_v) // \left[ 2 + R \frac{g_m}{1 + g_m R_1} \right] \right]$$

let  $g_m R_1 \gg 1$

$$R_{gd} = R \left[ (1 - A_v) // \left( 2 + \frac{R}{R_1} \right) \right] = R \left[ (1 - A_v) // (2 - A_v) \right]$$

let  $|A_v| \gg 1$  and  $|A_v| \gg 2$

$$R_{gd} = R \left[ +A_v // A_v \right] = -R \frac{+A_v \times A_v}{A_v + A_v} = -R \frac{A_v^2}{2A_v}$$

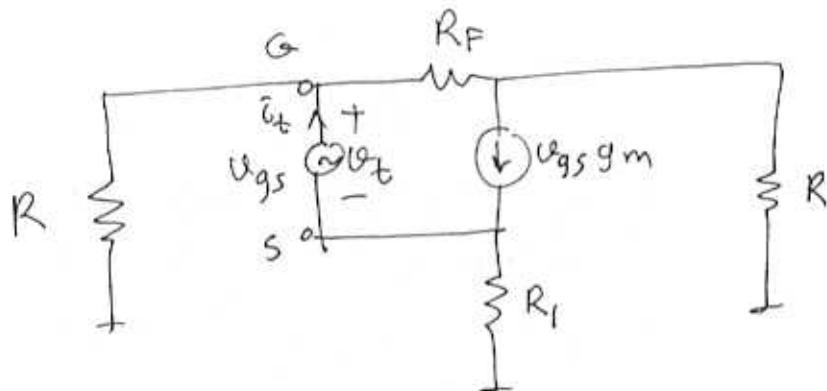
$$R_{gd} \approx -R \frac{A_v}{2}$$

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3

$$R_{gd} \approx R \frac{|Av|}{2}$$

$$\Rightarrow T_{gd} = C_{gd} \times R \frac{|Av|}{2}$$

In order to find  $R_{gs}$ , the circuit becomes:



We can connect a test source  $v_t$  and calculate it, the current passing through the source and then calculate  $R_{in}$  by

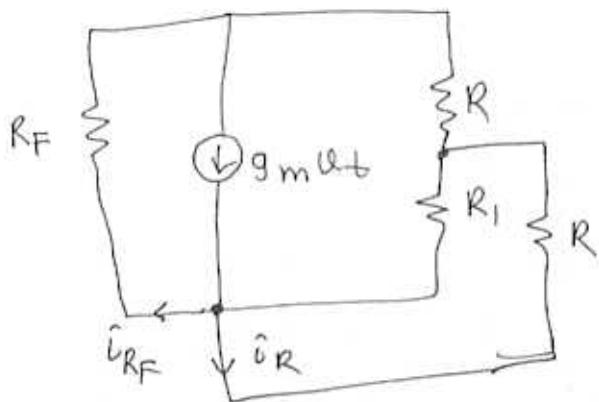
$$R_{in} = \frac{v_t}{i_t}$$

In order to find it we can use superposition to find the effects of  $v_t$  and  $v_{gs} g_m = v_t g_m$ . The contribution by  $v_t$  is given by

$$\begin{aligned} i_{g_t} &= v_t \times \frac{1}{(R_F + R) // R + R_1} = v_t \frac{1}{\frac{(R_F + R)R}{R_F + R + R} + R_1} \\ &= v_t \frac{R_F + 2R}{R_F R + R^2 + R_1 R_F + 2RR_1} \end{aligned}$$

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 (4)

The contribution by  $g_m v_{bt}$  can be calculated from the redrawn circuit:



$$\hat{i}_{g_c} = \hat{i}_{RF} + \hat{i}_R$$

$$\hat{i}_{RF} = g_m v_{bt} \cdot \frac{(R_1 // R) + R}{(R_1 // R) + R + R_F}$$

$$\hat{i}_R = g_m v_{bt} \frac{R_F}{(R_1 // R) + R + R_F} \cdot \frac{R_1}{R_1 + R}$$

$$\hat{i}_{g_c} = \hat{i}_{RF} + \hat{i}_R = g_m v_{bt} \frac{\frac{(R_1 // R) + R}{(R_1 // R) + R + R_F} + \frac{R_F R_1}{R_1 + R}}{(R_1 // R) + R + R_F}$$

$$= \frac{\frac{R_1 R}{R_1 + R} + \frac{R_F R_1}{R_1 + R} + \frac{R (R_1 + R)}{R_1 + R}}{\frac{R_1 R}{R_1 + R} + \frac{R (R_1 + R)}{R_1 + R} + \frac{R_F (R_1 + R)}{R_1 + R}} g_m v_{bt}$$

$$\hat{i}_{g_c} = g_m v_{bt} \frac{R R_1 + R_1 R_F + R R_1 + R^2}{R R_1 + R R_1 + R^2 + R_F R_1 + R_F R}$$

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(5)

$$i_t = i_{g_f} + i_{c_f} = v_t \frac{R_F + 2R}{RR_F + R^2 + R_1R_F + 2RR_1}$$

$$+ v_t g_m \frac{RR_1 + R_1R_F + RR_1 + R^2}{2RR_1 + R^2 + R_F R_1 + R_F R}$$

$$i_t = v_t \frac{R_F + 2R + g_m(2RR_1 + R_1R_F + R^2)}{R(2R_1 + R + R_F) + R_F R_1}$$

$$R_{eq} = \frac{v_t}{i_t} = \frac{R(2R_1 + R + R_F) + R_F R_1}{(R_F + 2R)(g_m R_1 + 1) + g_m R^2}$$

If component values are given  $R_{eq}$  can easily be calculated. But to get a general feeling about the BW of the amplifier  $R_{eq}$  can be simplified at large  $A_v$  to :

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5A

$$R_{eq} = \frac{R \left( 2 R_i \frac{R_F + R_E}{R_F - 1 - A_v} + R_F R_i \right) + R_F R_i}{\left( R_F + \frac{2 R_F}{1 - A_v} \right) g_m R_E + g_m R^2}$$

because  $R = \frac{R_F}{1 - A_v}$  and  $g_m R_E = 1 + g_m R_i$

$$R_{eq} = \frac{R_F \left[ R \left( \frac{2 R_i}{R_F} + \frac{1}{1 - A_v} + 1 \right) + R_i \right]}{R_F g_m \left[ \left( 1 + \frac{2}{1 - A_v} \right) R_E + \frac{R^2}{R_F} \right]}$$

but  $R_F = \frac{R^2}{R_E}$   
or  $R_E = \frac{R^2}{R_F}$

for large  $A_v$   $\frac{1}{1 - A_v} \ll 1$   $R_i < R_E \ll R \ll R_F$

$$R_{eq} = \frac{R + R_i}{g_m (R_E + R_F)} \approx \frac{R}{2 g_m R_E}$$

$$R_{eq} = \frac{R (1 - A_v)}{2 g_m R} \approx \frac{|A_v|}{2 g_m}$$

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⑥

$$\tau_{gs} = C_{gs} \times R_{gs} = C_{gs} \cdot \frac{R}{2R_E} \frac{1}{g_m} \approx C_{gs} \frac{|Av|}{2g_m}$$

Therefore the BW becomes

$$BW = \frac{1}{\tau_{gs} + \tau_{gd}} = \frac{1}{C_{gd} R \frac{|Av|}{2} + C_{gs} \frac{|Av|}{2g_m}}$$

$$BW \approx \left[ |Av| \left( \frac{C_{gs}}{2g_m} + \frac{RC_{gd}}{2} \right) \right]^{-1}$$

$$BW = \frac{1}{|Av|} \frac{1}{\frac{C_{gs}}{2g_m} + \frac{RC_{gd}}{2}} \Rightarrow$$

$$BW \times |Av| = \frac{1}{\frac{C_{gs}}{2g_m} + \frac{RC_{gd}}{2}}$$

different from the book  
 $\Rightarrow$  The gain-bandwidth product of the amplifier  
 is constant. And in practical cases  $C_{gd}$  dominates  
 the bandwidth.

For a typical small signal transistor which  
 we are using at the examples,

$$\left. \begin{aligned} \frac{C_{gs}}{2g_m} &= 9.16 \times 10^{-12} \\ \frac{C_{gd} R}{2} &= 13.5 \times 10^{-12} \end{aligned} \right\} \Rightarrow C_{gs} \text{ is not negligible and}$$

$$BW \times |Av| = 4.41 \times 10^{10}$$

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(7)

Assuming that the BW is mainly limited by one dominant pole at the input (remember the case at experiment II), i.e.

$$w_0 = \frac{1}{Z} = \frac{1}{R C_{in}} = \frac{1}{|A_v| \frac{C_{gs}}{2g_m} + |A_v| \frac{R C_{gd}}{2}}$$

$$\cancel{R} C_{in} = \cancel{\frac{R}{R_i}} \frac{C_{gs}}{2g_m} + \frac{R C_{gd}}{2} |A_v|$$

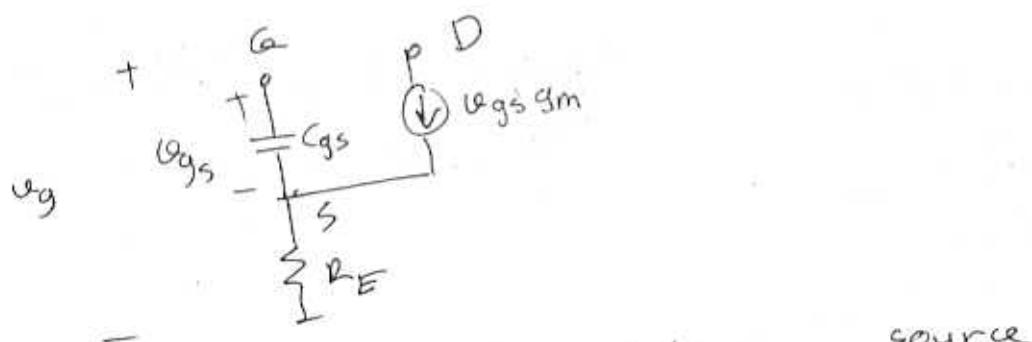
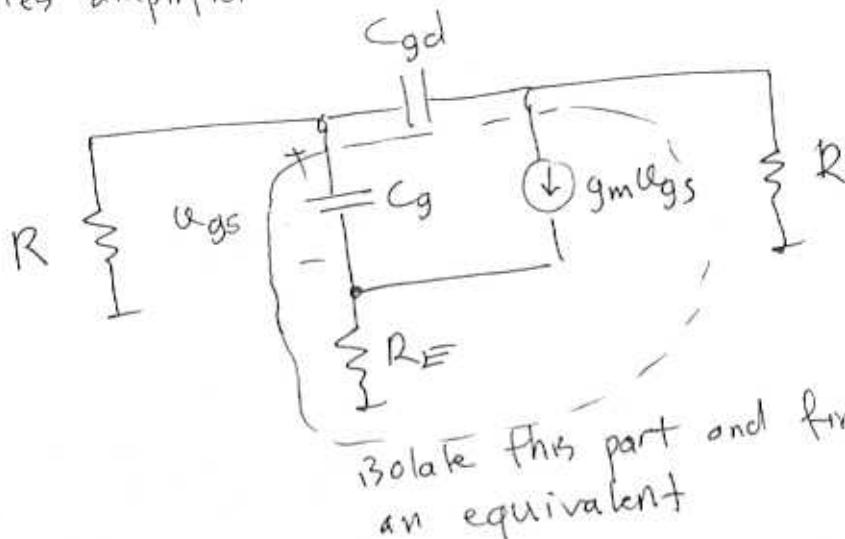
$$C_{in} \approx \frac{C_{gs}}{2R_i g_m} + C_{gd} \frac{|A_v|}{2}$$

in practical cases  $C_{gd} \left( \frac{|A_v|}{2} \right)$  dominates the input impedance

Formulation to find out the exact expression of  $R_o$  of the shunt-series amplifier

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(1)



writing the node equation at the source

$$v_s G_E = (v_g - v_s) s C_{gs} + (v_g - v_s) g_m$$

$$v_s G_E = v_g (s C_{gs} + g_m) - v_s (s C_{gs} + g_m)$$

$$v_s [G_E + g_m + s C_{gs}] = v_g [s C_{gs} + g_m]$$

$$\Rightarrow v_s = v_g \frac{[s C_{gs} + g_m]}{G_E + g_m + s C_{gs}}$$

$$i_g = s C_{gs} [v_g - v_s] \Rightarrow$$

$$Z_{in} = \frac{v_g}{i_g} = \frac{v_g}{s C_{gs} [v_g - v_g \frac{[s C_{gs} + g_m]}{G_E + g_m + s C_{gs}}]} \\ \downarrow s C_{gs} [v_g - v_s]$$

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(2)

$$Z_{in} = \frac{1}{sC_{gs} \left[ 1 - \frac{g_m + sC_{gs}}{G_E + sC_{gs} + g_m} \right]}$$

$$= \frac{1}{sC_{gs} \left[ \frac{G_E + sC_{gs} + g_m - g_m - sC_{gs}}{G_E + sC_{gs} + g_m} \right]}$$

$$= \frac{G_E + g_m + sC_{gs}}{sC_{gs} G_E} = \frac{G_E + g_m}{sC_{gs} G_E} + \frac{1}{G_E}$$

$$Z_{in} = \frac{1 + \frac{g_m}{G_E}}{sC_{gs}} + R_E = \underbrace{\frac{1 + g_m R_E}{C_{gs}}}_{C_{eq.}} \cdot \frac{1}{s} + R_E$$

$$Z_{in} = \frac{1}{sC_{eq}} + R_E \quad \text{where } C_{eq} = \frac{C_{gs}}{1 + g_m R_E}$$

$$i_d = v_{gs} g_m = g_m (v_g - v_s) = g_m v_g \left[ 1 - \frac{sC_{gs} + g_m}{G_E + g_m + sC_{gs}} \right]$$

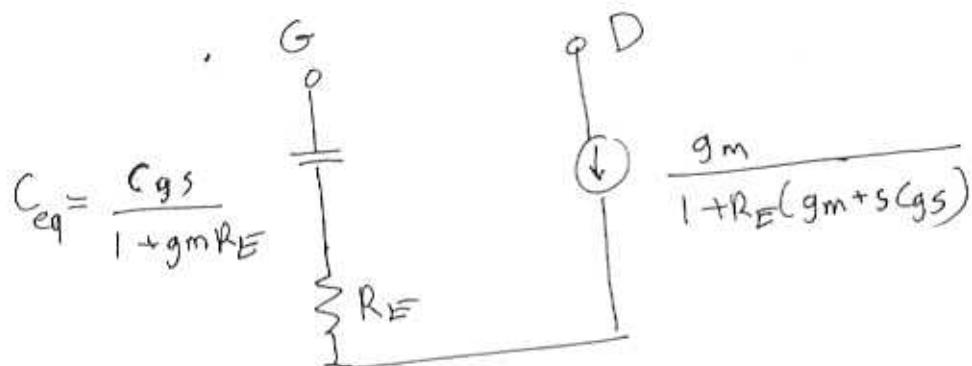
$$\bar{i}_d = v_g g_m \frac{G_E + g_m + sC_{gs} - sC_{gs} - g_m}{G_E + g_m + sC_{gs}}$$

$$\bar{i}_g = v_g \frac{g_m G_E}{G_E + g_m + sC_{gs}} = v_g g_m \frac{1}{1 + g_m R_E + sC_{gs} R_E}$$

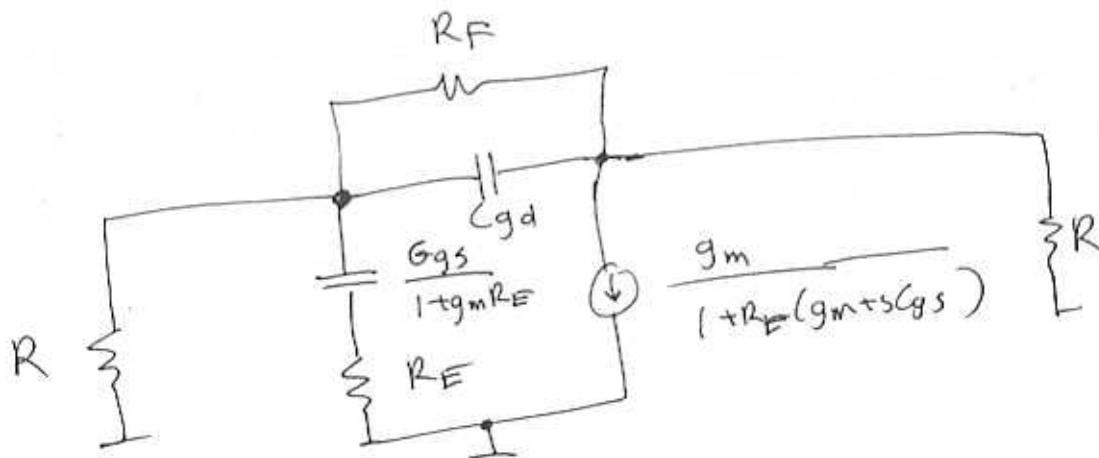
$$\bar{i}_g = v_g \frac{g_m}{\dots n - r_a + c(cac)}$$

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(3)

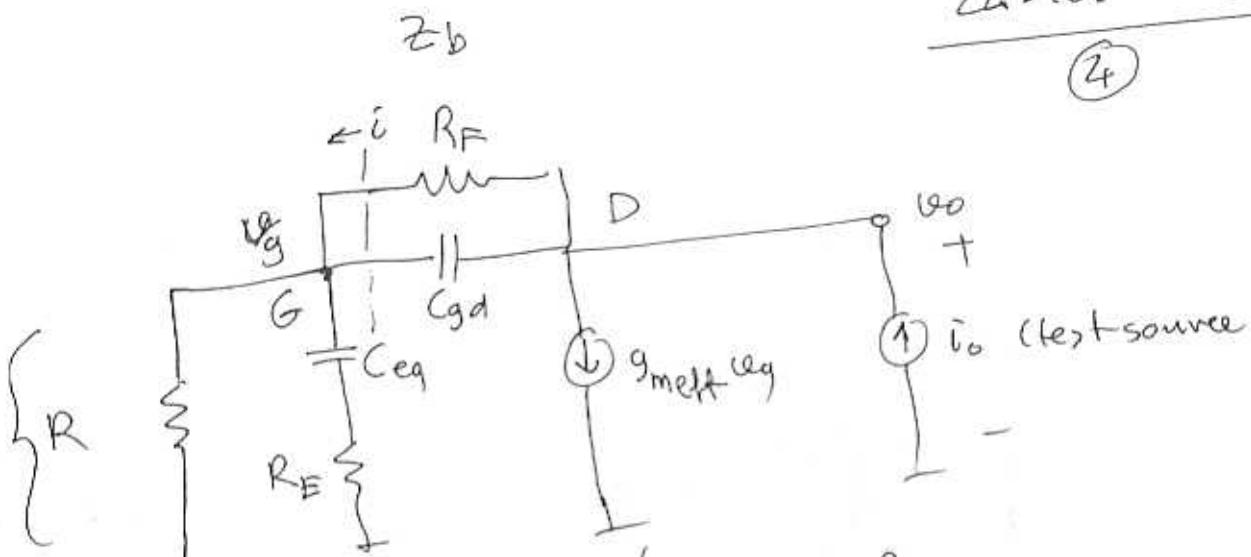


Substituting into the original diagram



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(4)



$$Z_B = R_F \parallel \frac{1}{sC_{gd}} = \frac{R_F \cdot \frac{1}{sC_{gd}}}{R_F + \frac{1}{sC_{gd}}} = \frac{R_F}{1 + R_F s C_{gd}}$$

$$Z_A = R \parallel \left( R_E + \frac{1}{sC_{eq}} \right) = \frac{R \left( R_E + \frac{1}{sC_{eq}} \right)}{R + R_E + \frac{1}{sC_{eq}}} = R \frac{\left[ sC_{eq} R_E + 1 \right]}{(R + R_F) s C_{eq} + 1}$$

$$Z_A = R$$

$$i = i_o - v_g g_{m\text{eff}}$$

$$i Z_A = v_g = Z_A (i_o - v_g g_{m\text{eff}})$$

$$v_g = Z_A i_o - Z_A v_g g_{m\text{eff}}$$

$$v_g (1 + Z_A g_{m\text{eff}}) = Z_A i_o \Rightarrow$$

$$\boxed{v_g = i_o \frac{Z_A}{1 + Z_A g_{m\text{eff}}}}$$

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⑤

$$i [z_a + z_b] = v_0$$

$$v_0 = [z_a + z_b] [i_0 - v_g g_{\text{melt}}]$$

$$v_0 = [z_a + z_b] \left[ i_0 - v_g g_{\text{melt}} \cdot \frac{z_a}{1 + z_a g_{\text{melt}}} \right]$$

$$R_0 = \frac{v_0}{i_0} = [z_a + z_b] \left[ 1 - g_{\text{melt}} \frac{z_a}{1 + z_a g_{\text{melt}}} \right]$$

$$= [z_a + z_b] \left[ \frac{1 + z_a g_{\text{melt}} - z_a g_{\text{melt}}}{1 + z_a g_{\text{melt}}} \right]$$

$$= [z_a + z_b] \frac{1}{1 + z_a g_{\text{melt}}}$$

$$R_0 = \frac{z_a + z_b}{1 + z_a g_{\text{melt}}}$$

$$= \frac{z_a + z_b}{1 + z_a \frac{g_m}{1 + R_E(g_m + sC_{gs})}}$$

$$\frac{sC_{gs}R_E}{1+g_mR_E} + 1$$

$$Z_a = R \frac{(R+R_E) \frac{sC_{gs}}{1+g_mR_E} + 1}{sC_{gs}R_E + 1}$$

$$= R \frac{\frac{R_E sC_{gs} + 1 + g_m R_E}{1 + g_m R_E}}{\frac{(R+R_E)sC_{gs} + 1 + g_m R_E}{1 + g_m R_E}}$$

$$= R \frac{\frac{R_E sC_{gs} + 1 + g_m R_E}{(R+R_E)sC_{gs} + 1 + g_m R_E}}{\frac{sC_{gs} + G_E + g_m}{R + R_E}} = R R_E \frac{\frac{sC_{gs} + G_E + g_m}{sC_{gs} + G_E + g_m}}{\frac{R + R_E}{R_E}}$$

$$Z_a = R \frac{\frac{sC_{gs} + G_E + g_m}{(1 + \frac{R}{R_E})sC_{gs} + G_E + g_m}}{\frac{sC_{gs} + G_E + g_m}{sC_{gs} + G_E + g_m}}$$

$$R_o = \frac{(Z_a + Z_b) - \frac{1}{1 + R_E(g_m + sC_{gs}) + Z_a g_m}}{1 + R_E(g_m + sC_{gs})}$$

$$R_o = \frac{(Z_a + Z_b)(1 + R_E(g_m + sC_{gs}))}{1 + R_E(g_m + sC_{gs}) + Z_a g_m}$$

$$R_o = \frac{\left[ R \frac{sC_{eq}R_E + 1}{(R + R_E)sC_{eq} + 1} + \frac{R_F}{1 + R_F sC_{gd}} \right]}{1 + R_E(g_m + sC_{gs}) + g_m R \frac{sC_{eq}R_E + 1}{(R + R_E)sC_{eq} + 1}}$$

$$R_o = \frac{R \left[ \frac{s \frac{C_{gs} R_F}{1 + g_m R_E} + 1}{(R + R_E)s \frac{C_{gs}}{1 + g_m R_E} + 1} + \frac{R_F}{1 + R_F s C_{gd}} \right]}{1 + R_E(g_m + sC_{gs}) + g_m R \left[ \frac{s \frac{C_{gs} R_E}{1 + g_m R_E}}{(R + R_E)s \frac{C_{gs}}{1 + g_m R_E} + 1} \right]}$$

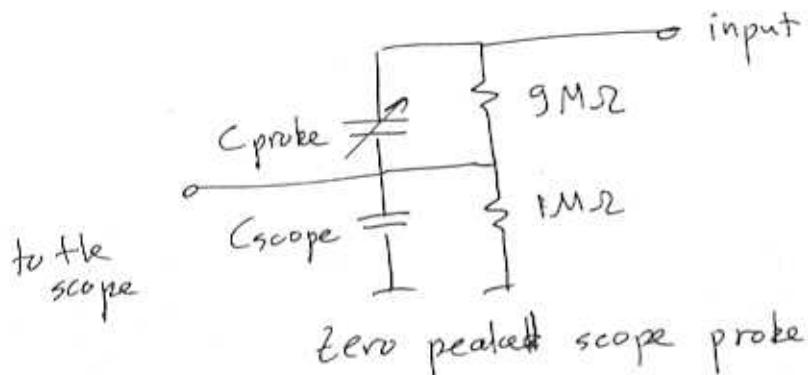
$$Z_o = \frac{1}{1 + R_E(g_m + sC_{gs}) + g_m R \left[ \frac{s \frac{C_{gs} R_E}{1 + g_m R_E}}{(R + R_E)s \frac{C_{gs}}{1 + g_m R_E} + 1} \right]}$$

$$R_o = \frac{R \frac{sC_{gs} + G_E + g_m}{\left(1 + \frac{R}{R_E}\right)sC_{gs} + G_E + g_m} + R_F \frac{1}{G_F + sC_{gd}}}{1 + R_E(g_m + sC_{gs}) + g_m R \frac{sC_{gs} + G_E + g_m}{\left(1 + \frac{R}{R_E}\right)sC_{gs} + G_E + g_m}}$$

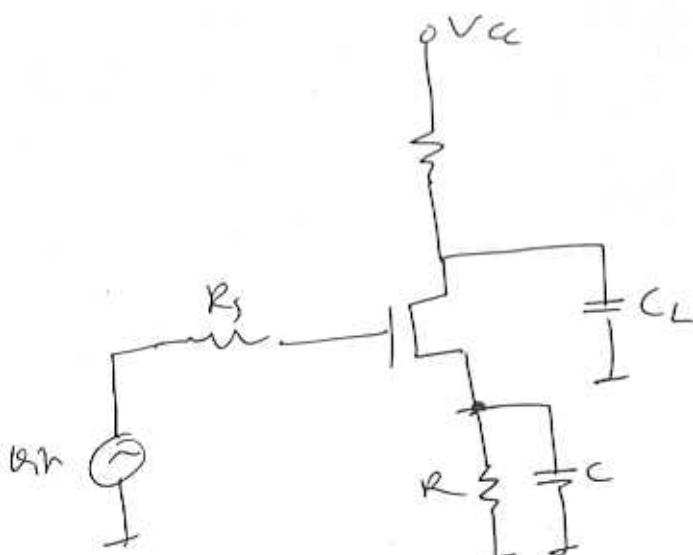
18.10.2005

(2)

Talk about scope probe



zero-peaked scope probe



zero-peaked common source amplifier