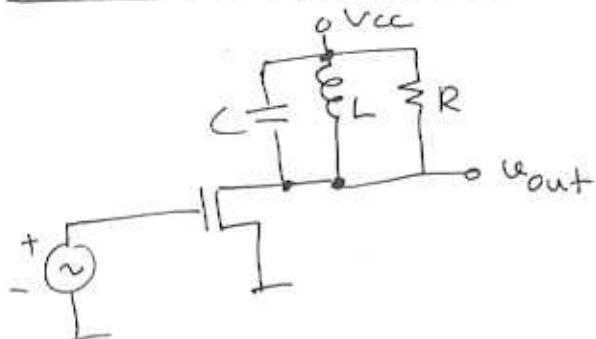


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### Tuned amplifiers



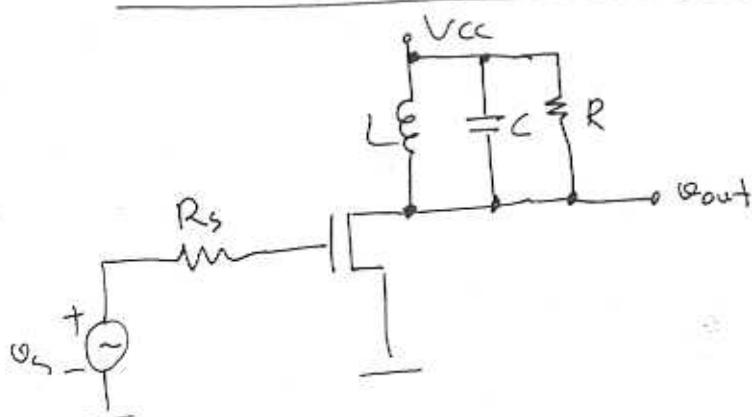
In the case where the amplifier is driven by an ideal voltage source,  $C_{gd}$  is absorbed into  $C$ , therefore at resonance:

$$\text{Gain} = g_m R$$

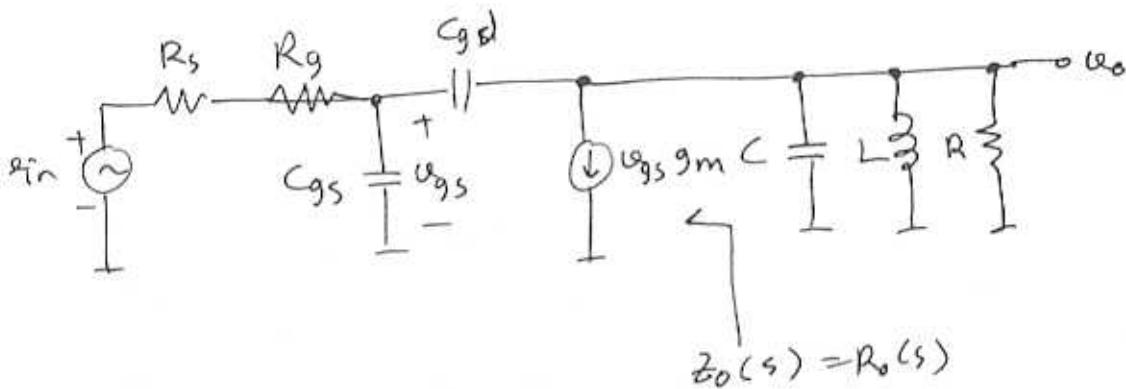
$$\frac{\text{BW}}{\omega_0} = \frac{1}{Q} = \frac{1}{\omega_0 RC} \Rightarrow \text{BW} = \frac{1}{RC}$$

$$\text{Gain} \times \text{BW} = \frac{g_m R}{RC} = \frac{g_m}{C}$$

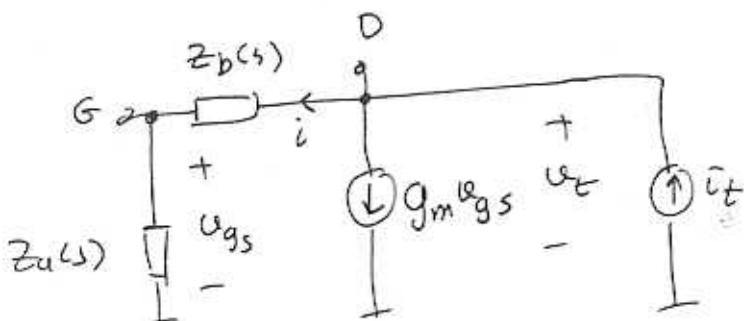
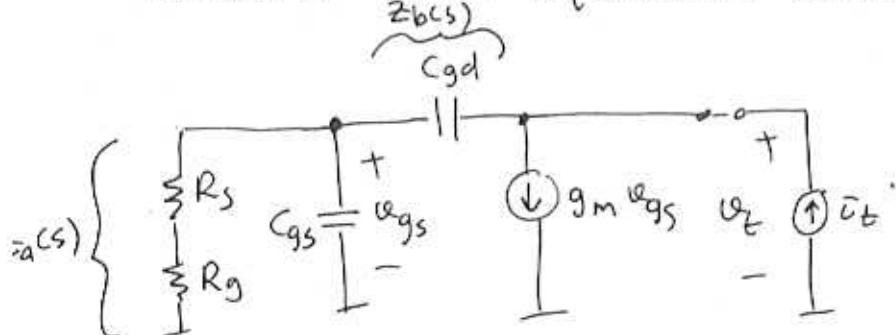
### Detailed design of the tuned amplifier



The small signal model is:



In order to analyse the circuit, we must find the loading our transistor creates on the tank circuit. The equivalent circuit to find  $R_o(s)$  is:



$$i = \bar{i}_t - g_m v_{gs}$$

$$\bar{i} Z_d(s) = v_{gs} = Z_a(s) [\bar{i}_t - v_{gs} g_m]$$

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⑥

$$v_{gs} [1 + Z_a(s) g_m] = Z_a(s) i_t$$

$$v_{gs} = \frac{Z_a(s)}{1 + Z_a(s) g_m} i_t$$

But

$$i [Z_a(s) + Z_b(s)] = v_t \Rightarrow$$

$$v_t = [Z_a(s) + Z_b(s)] [\bar{i}_t - g_m v_{gs}]$$

$$= [Z_a(s) + Z_b(s)] \left[ \bar{i}_t - g_m \frac{Z_a(s) i_t}{1 + Z_a(s) g_m} \right]$$

$$Z_0(s) = \frac{v_t}{\bar{i}_t} = [Z_a(s) + Z_b(s)] \left[ \frac{1 + Z_a(s) g_m - g_m Z_a(s)}{1 + Z_a(s) g_m} \right]$$

$$Z_0(s) = \frac{Z_a(s) + Z_b(s)}{1 + Z_a(s) g_m}$$

$$Z_a(s) = \frac{(R_s + R_g) \cdot \frac{1}{j\omega C_{gs}}}{R_s + R_g + \frac{1}{j\omega C_{gs}}} = \frac{R_s + R_g}{1 + (R_s + R_g) j\omega C_{gs}}$$

$$Z_b(s) = \frac{1}{j\omega C_{gd}}$$

(which means that we are well below cutoff)  
ignoring  $C_{gs}$   $Z_a(s)$  becomes  $R_s + R_g$

$$\Rightarrow Z_0(s) = \frac{R_s + R_g + \frac{1}{s C_{gd}}}{1 + (R_s + R_g) g_m} = \frac{R_s + R_g}{1 + (R_s + R_g) g_m} + \frac{1}{s C_{gd} [1 + (R_s + R_g) g_m]}$$

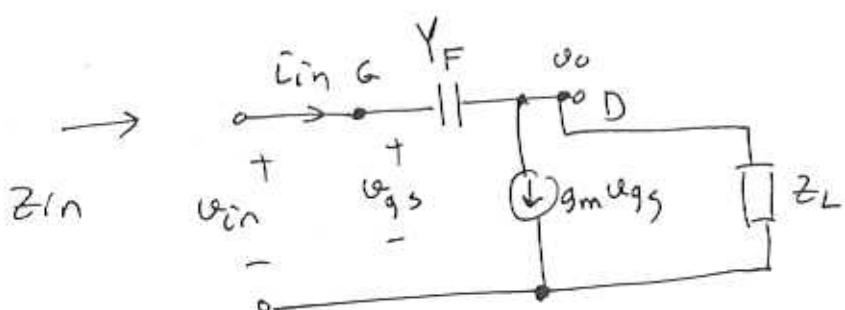
$\Rightarrow$  The reactive part of  $Z_0(s)$  is created by  
 $C_{gd} [1 + (R_s + R_g) g_m]$

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It means that the miller effect loads the output tank multiplied by  $1 + (R_s + R_g)g_m$

Therefore the resonant frequency of the tank is dependant on  $C_{gd}$ . Since it varies ~~on~~ depending on different parameters it must be kept low compared to the capacitance of the tank circuit.

A more serious effect of the miller capacitance on the tuned amplifier comes from the input impedance of the amplifier. Let us find the input impedance of the amplifier excluding  $C_{gs}$ :



$$\begin{aligned} i_{in} &= (v_{gs} - v_o) Y_F \\ v_o &= (i_{in} - g_m v_{gs}) Z_L \end{aligned} \quad \Rightarrow \quad i_{in} = Y_F [v_{gs} - Z_L (i_{in} - g_m v_{gs})]$$

$$\Rightarrow i_{in} = Y_F v_{gs} - Y_F Z_L i_{in} + Y_F Z_L g_m v_{gs}$$

$$i_{in} [1 + Y_F Z_L] = Y_F v_{gs} [Z_L g_m + 1]$$

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$$Y_{in} = \frac{i_{in}}{v_{gs}} = \frac{i_{in}}{v_{in}} = (Y_F + Y_F Z_L g_m) / (1 + Y_F Z_L)$$

If  $Z_F \gg Z_L$  as in a properly designed amplifier

$$\Rightarrow 1 + Y_F Z_L = 1 + \frac{Z_L}{Z_F} \approx 1 \Rightarrow$$

$$Y_{in} = Y_F + Y_F Z_L g_m$$

At this point we can add  $C_{gs}$  to the picture and write  $Z_L = R_L + jX_L \Rightarrow$

$$\begin{aligned} Y_{in} &= j\omega [C_{gs} + C_{gd}] + j\omega C_{gd}[R_L + jX_L]g_m \\ &= j\omega [C_{gs} + C_{gd}[1 + g_m R_L]] - \omega C_{gd}(g_m X_L) \\ &= -\omega C_{gd} g_m X_L + j\omega [C_{gs} + C_{gd}(1 + R_L g_m)] \end{aligned}$$

Notice here that:  
1-) if the load impedance is inductive (i.e.  $X_L > 0$ ), then the input impedance has a negative real part

2-)  $C_{gd}$  is reflected to input multiplied by  $(1 + g_m R_L)$

Corollaries:

1-) The resistive part of the source admittance must be large enough to prevent oscillation at the frequencies where  $X_L$  is positive (inductive). Note that  $Z_L$  is inductive if  $\omega < \frac{1}{(LC)^{1/2}} = \omega_0$

2o

$$Z_o(j\omega) = \frac{R_s + R_g}{1 + (R_s + R_g)g_m} + \frac{1}{j\omega C_{gd} [1 + (R_s + R_g)g_m]}$$

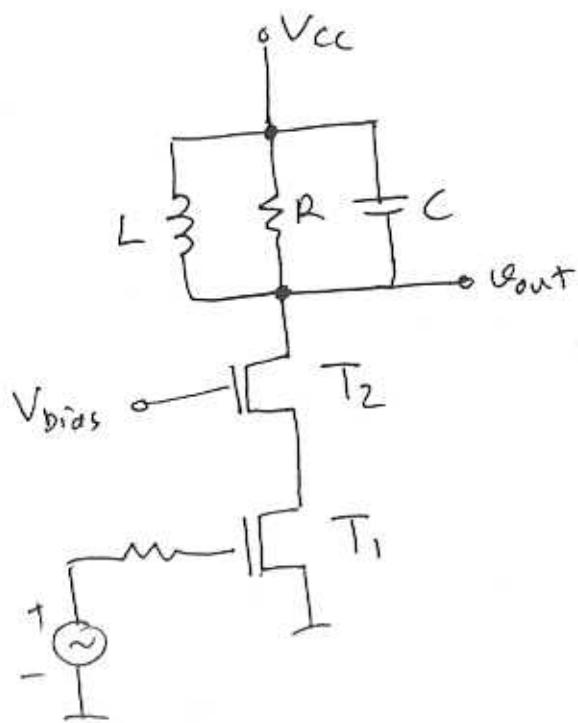
$$Y_{in}(j\omega) = -w C_{gd} g_m X_L + jw [C_{gs} + C_{gd}(1 + R_L g_m)]$$

Again notice here that at both loadings

$C_{gd}$  is multiplied by a factor related to the gain of the transistor, i.e.  $(1 + R_L g_m)$  or  $[1 + (R_s + R_g)g_m]$

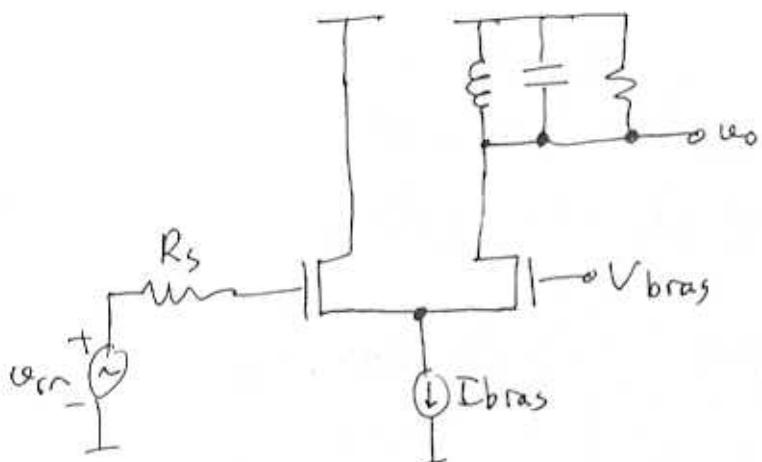
### Unilateralization and Neutralization

The effect of the miller capacitance  $C_{gd}$  can again be mitigated by cascode configuration which effectively ground  $C_{gd2}$  &  $C_{gdi}$ .

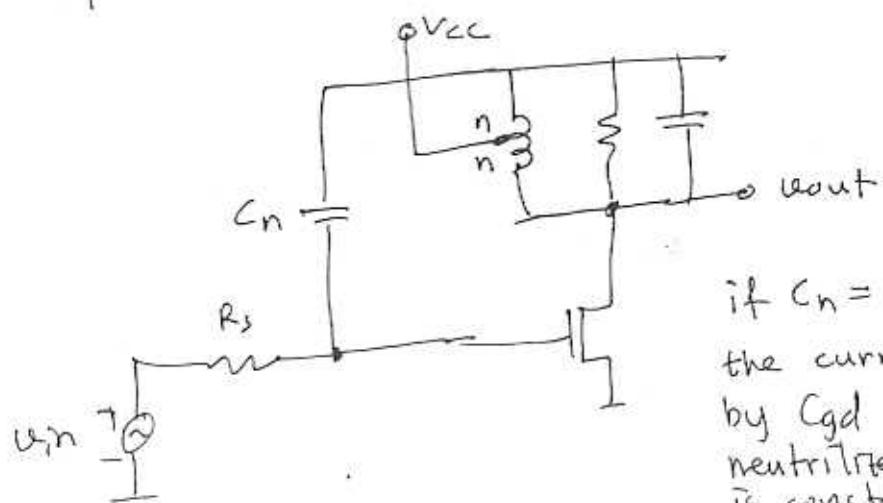


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Or by the use of a source follower input amplifier followed by a common-gate configuration which also effectively ground both  $C_{gd1}$  and  $C_{gd2}$ .



We can call these two amplifiers as unilateral amplifiers since the signal flow in one direction from one amplifier to the other. One other method which cancels the effect of the Miller capacitance is neutralization.

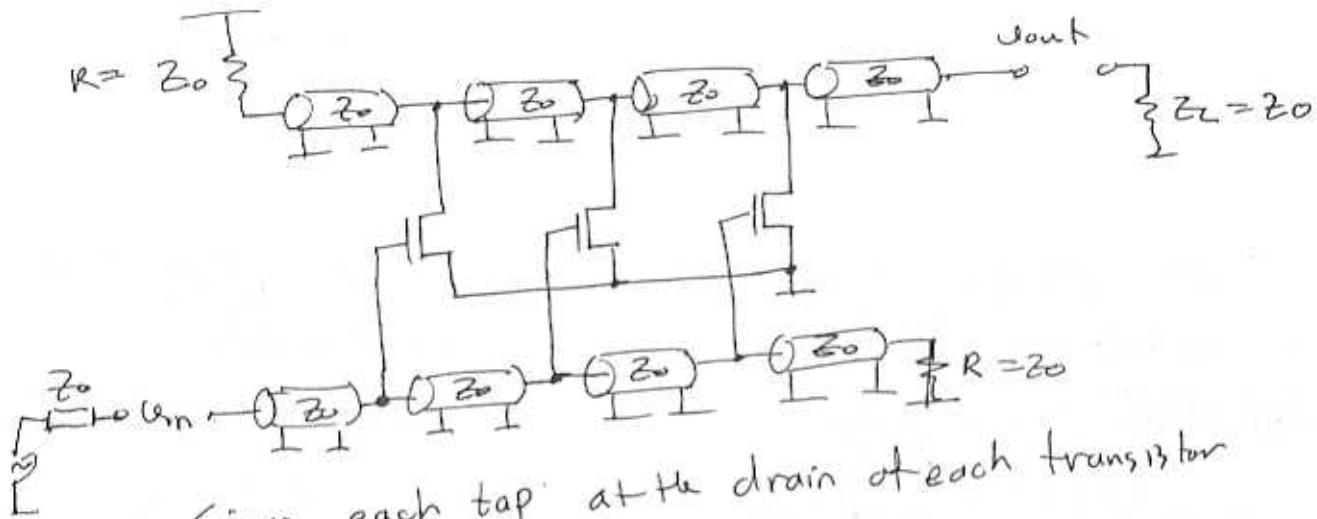


if  $C_n = C_{gd}$   
 the current coupled by  $C_{gd}$  is completely  
 neutralized if  $C_{gd}$   
 is constant.

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## The distributed amplifier



Since each tap at the drain of each transistor shows an impedance of  $Z_0/2$  and since delay from input to the output through each transistor is the same (add the output voltages created by each transistor since they are in phase)

$$V_o = n g_m \frac{Z_0}{2} V_{in} \quad (1)$$

$$\text{gain} = \frac{V_o}{V_{in}} = n g_m \frac{Z_0}{2} \text{ so gain increase}$$

with  $n$ , which means that even individual gains less than one can be combined to obtain gains substantially greater than one with suitable  $n$ . Trading delay with bandwidth.

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8-A

The condition for oscillation is:

$$\frac{G_S}{\text{G}_S} + (-wC_{gd}g_m X_L) < 0$$

$$\frac{G_S}{\text{G}_S} < wC_{gd}g_m X_L$$

$$\frac{1}{wC_{gd}g_m X_L} < \frac{1}{\text{G}_S} = R_S$$

$$R > \frac{1}{wC_{gd}g_m X_L}$$

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8-B

$$\begin{aligned}
 Y_{in} &= \frac{Y_F + Y_F Z_L g_m}{1 + Y_F Z_L} = \frac{1 + Z_L g_m}{\frac{1}{Y_F} + Z_L} \\
 &= \frac{1 + Z_L g_m}{Z_F + Z_L} = \frac{1 + (R + jX) g_m}{\frac{1}{jwC_{gd}} + R + jX} \\
 &= \frac{(1 + R g_m) + j X g_m}{R + j(X - \frac{1}{wC_{gd}})} = \boxed{(1 + R g_m) + j X g_m} \\
 &\boxed{\frac{[(1 + R g_m) + j X g_m] [R - j(X - \frac{1}{wC_{gd}})]}{R^2 + (X - \frac{1}{wC_{gd}})^2}} \\
 Y_{in} &= \frac{[(1 + R g_m) R + X g_m (X - \frac{1}{wC_{gd}})] + j(R X g_m + (1 + R g_m)(\frac{1}{wC_{gd}} X))}{R^2 + (X - \frac{1}{wC_{gd}})^2} + \frac{-j}{wC_{gs}}
 \end{aligned}$$

$$(1 + R g_m) R - X g_m (\frac{1}{wC_{gd}} - X) < 0 \Rightarrow \text{oscillation}$$

$$(1 + R g_m) R > X g_m (\frac{1}{wC_{gd}} - X) \Rightarrow \begin{matrix} \text{stability} \\ \text{stability} \end{matrix} \quad //$$

$$\begin{aligned}
 (1 + g_m R) R < g_m \frac{X}{wC_{gd}} - g_m X^2 &\Rightarrow // \\
 (1 + g_m R) R > g_m \frac{X}{wC_{gd}} - g_m X^2 &\Rightarrow \text{stability} \\
 \Rightarrow \text{stability} &\\
 \Rightarrow \text{stability} &
 \end{aligned}$$

$$g_m X^2 - \frac{g_m}{wC_{gd}} X + (1 + g_m R) R > 0$$

$$\begin{aligned}
 X^2 + X_c X + \underbrace{\frac{1 + g_m R}{g_m} R}_{c = } &> 0 \\
 a = 1 & \\
 b = X_c & \\
 c = &
 \end{aligned}$$

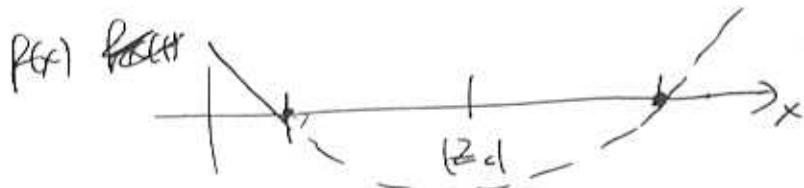
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$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} = +\left(\frac{-b}{2a}\right) \pm \sqrt{\left(\frac{b}{2a}\right)^2 - \frac{c}{a}} = +\left(\frac{-b}{2}\right) \pm \sqrt{\left(\frac{-b}{2}\right)^2 - c}$$

if  $a=1$

$$= +\left(\frac{-X_c}{2}\right) \pm \sqrt{\left(\frac{-X_c}{2}\right)^2 - \frac{1+g_m R}{g_m} R}$$

$$= \frac{1}{2w(C_d)} \pm \sqrt{\left(\frac{1}{2w(C_d)}\right)^2 - \frac{1+g_m R}{g_m} R}$$



$$\Rightarrow x < \frac{1}{2w(C_d)} - \sqrt{\left(\frac{1}{2w(C_d)}\right)^2 - \frac{1+g_m R}{g_m} R}$$

and

$$x > \frac{1}{2w(C_d)} + \sqrt{\left(\frac{1}{2w(C_d)}\right)^2 - \frac{1+g_m R}{g_m} R}$$