

## Overlap and Add Method:

Overlap and add method is based on the linearity of the

convolution:  $y[n] = (x_1[n] + x_2[n] + x_3[n]) * h[n]$

$$y[n] = x_1[n] * h[n] + x_2[n] * h[n] + x_3[n] * h[n].$$

Let  $x[n]$  be a long signal (or it may be streaming):

$x_j$  - The signal  $x[n]$  can be expressed as

$$x[n] = x_1[n] + x_2[n] + x_3[n]$$

where  $x_1[n]$  is ~~zero~~  $= x[n] w[n] = [x[0], x[1], \dots, x[\frac{L-1}{L}]]$

$$x_2[n] = x[n] w[n-L] = [x[L], x[L+1], \dots, x[2L-1]]$$

and

$$x_3[n] = x[n] w[n-2L] = [x[2L], x[2L+1], \dots, x[3L-1]]$$

Notice that  $w[n]$  is a window of length  $L$ :

$$w[n] = \begin{cases} 1, & n=0, 1, \dots, L-1 \\ 0, & \text{otherwise.} \end{cases}$$

The convolutions

$$y_i[n] = x_i[n] * h[n], \quad i=1, 2, \dots$$

have a length of  $L+M-1$ ;  $h[n]$  has a length of  $M$ .

We can use  $N \geq L+M-1$  length FFT to compute  $y_i[n]$  by computing  $y_i[n]$ ,  $i=1, 2, \dots$

$$y[n] = y_1[n] + y_2[n] + y_3[n] + \dots \quad (*)$$

Therefore, the input signal  $x[n]$  is divided into windows of length  $L$ . After using  $N$ -point DFT's we obtain  $y_1[n], y_2[n], \dots$

Since the starting points of  $y_1[n]$  is 0,  $y_2[n]$  is  $L$ ,  $y_3[n]$  is  $2L$ , the method is called "overlap and add" method.