

MATH206 Homework1 Solutions

1.

- a. 0.9473π
- b. -0.1959π
- c. -0.8701π

```
function argz = ArgZ(z1,z2,op)

argz1 = 180*(angle(z1)/pi);
argz2 = 180*(angle(z2)/pi);

if op == 1 % multiplication
    argz = argz1 + argz2;
else % division
    argz = argz1 - argz2;
end

if argz > 180 && argz < 360
    argz = argz - 360;
end

if argz > 360
    argz = mod(argz,360);
end

argz = argz/180; % convert to radians
```

2.

a.

```
solve(z^3-(1-2i)*z^2-(21+25i)*z-(124+32i))
```

```
ans =
```

```
-4-5*i
```

```
7+i
```

```
-2+2*i
```

b.

```
root = roots([2 0 -1 0 -1 0 3 0 2])
```

```
plot(root,'rx','MarkerSize',7)
```

```
grid
```

```
title('Root Plot')
```

```
xlabel('The real axis')
```

```
ylabel('The imaginary axis')
```

```
root =
```

```
-1.0755 + 0.4232i
```

```
-1.0755 - 0.4232i
```

```
1.0755 + 0.4232i
```

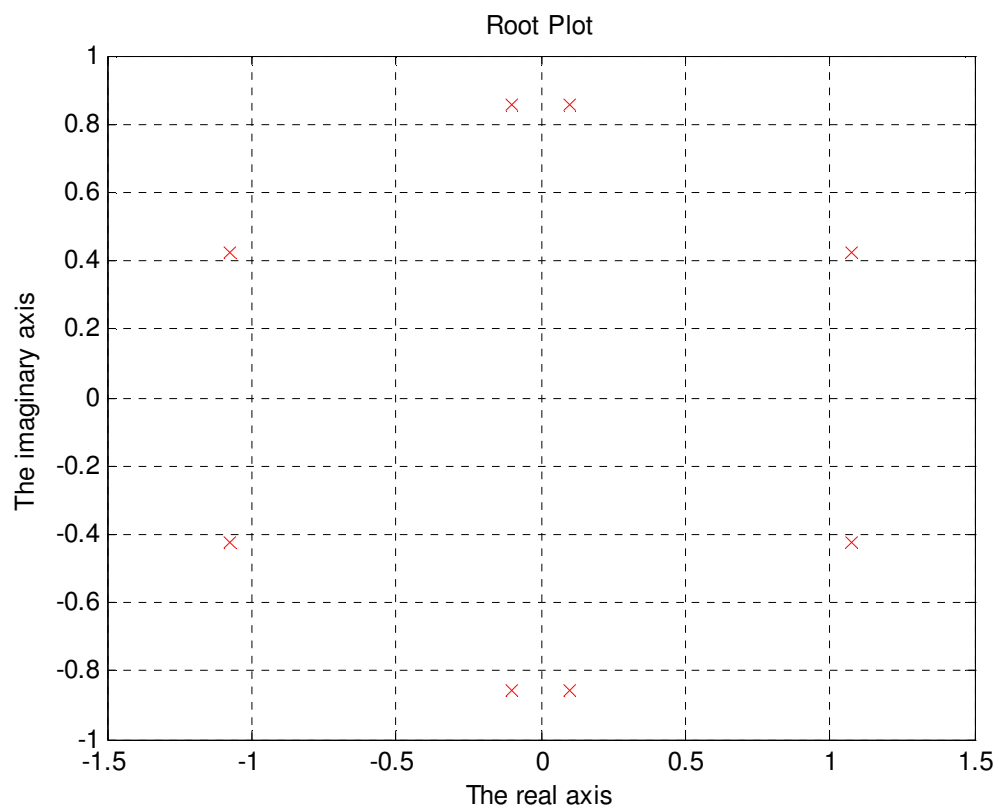
```
1.0755 - 0.4232i
```

```
-0.1029 + 0.8591i
```

```
-0.1029 - 0.8591i
```

```
0.1029 + 0.8591i
```

```
0.1029 - 0.8591i
```



3.

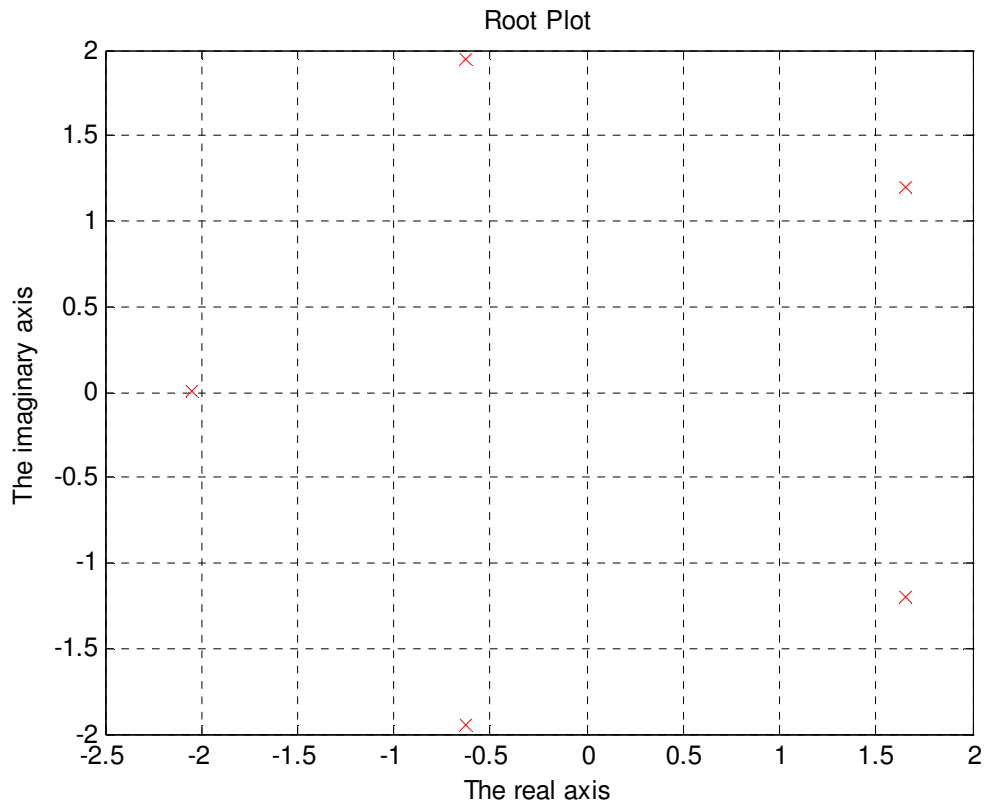
```
function allroots = FindRoots(z0,n)
P_Zo = phase(z0);
Ab_Zo = abs(z0);
allroots = zeros(1,n);
for k = 0:n-1,
    allroots(k+1) = (Ab_Zo^(1/n))*exp(i*(P_Zo+2*pi*k)/n);
end
figure
plot(allroots,'rx','MarkerSize',7)
grid on
title('Root Plot')
xlabel('The real axis')
ylabel('The imaginary axis')
```

a.

```
>> FindRoots(-36,5)
```

```
ans =
```

```
1.6566 + 1.2036i -0.6328 + 1.9475i -2.0477 + 0.0000i -0.6328 - 1.9475i 1.6566 - 1.2036i
```



b.

```
FindRoots(-27*sqrt(3)-i*27,8)
```

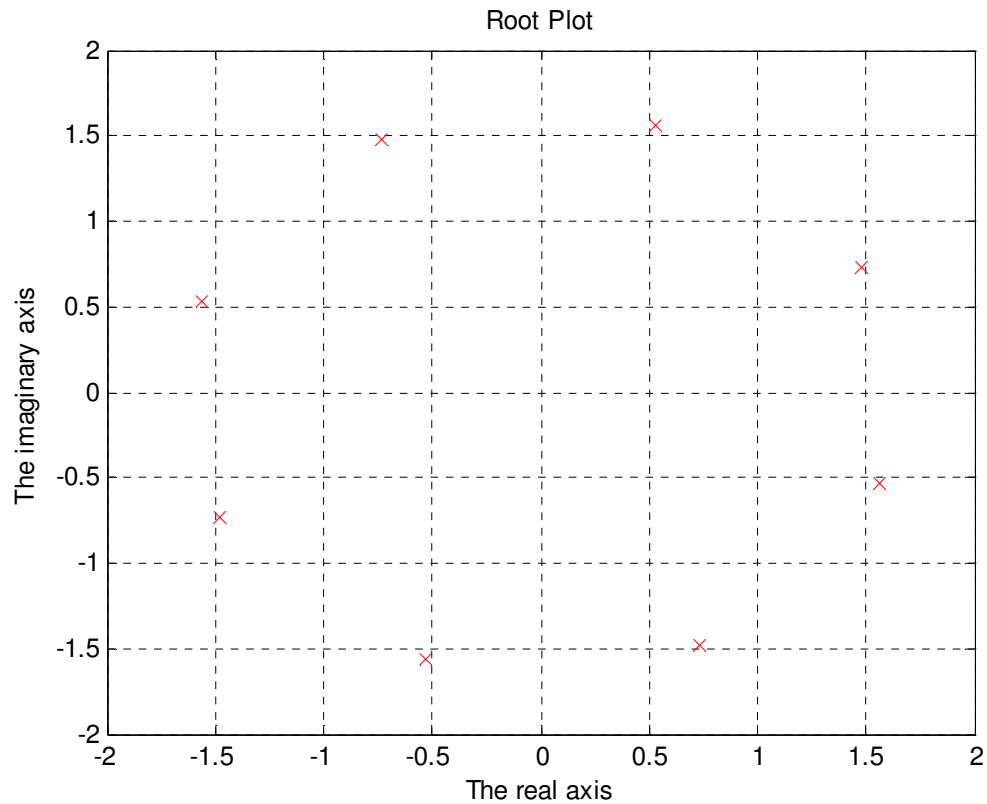
```
ans =
```

```
Columns 1 through 5
```

```
1.5591 - 0.5292i 1.4767 + 0.7282i 0.5292 + 1.5591i -0.7282 + 1.4767i -1.5591 + 0.5292i
```

Columns 6 through 8

-1.4767 - 0.7282i -0.5292 - 1.5591i 0.7282 - 1.4767i



4.

```
clear all;close all;clc
```

```
% assume our complex region is defined by  $z = x + i*y$ 
```

```
l = 0;  
for x = 0:0.01:1,  
    for y = -2*x:0.01:2*x,  
        l = l+1;  
        z(l) = x+i*y;  
    end  
end
```

```
w = exp(z);  
% w = sin(z);
```

```
subplot(1,2,1)  
plot(z)  
grid on  
xlabel('The real axis')  
ylabel('The imaginary axis')  
title('The input region')
```

```
subplot(1,2,2)
plot(w)
grid on
xlabel('The real axis')
ylabel('The imaginary axis')
title('The transformed region')
```

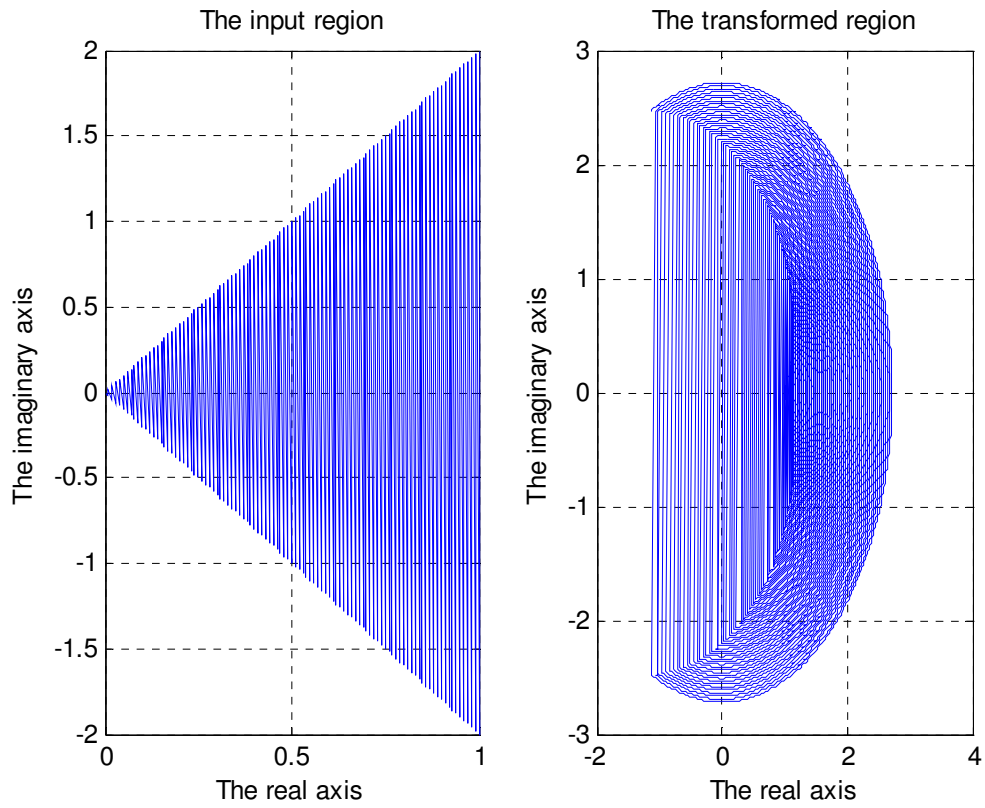


Figure 1. $w = \exp(z)$

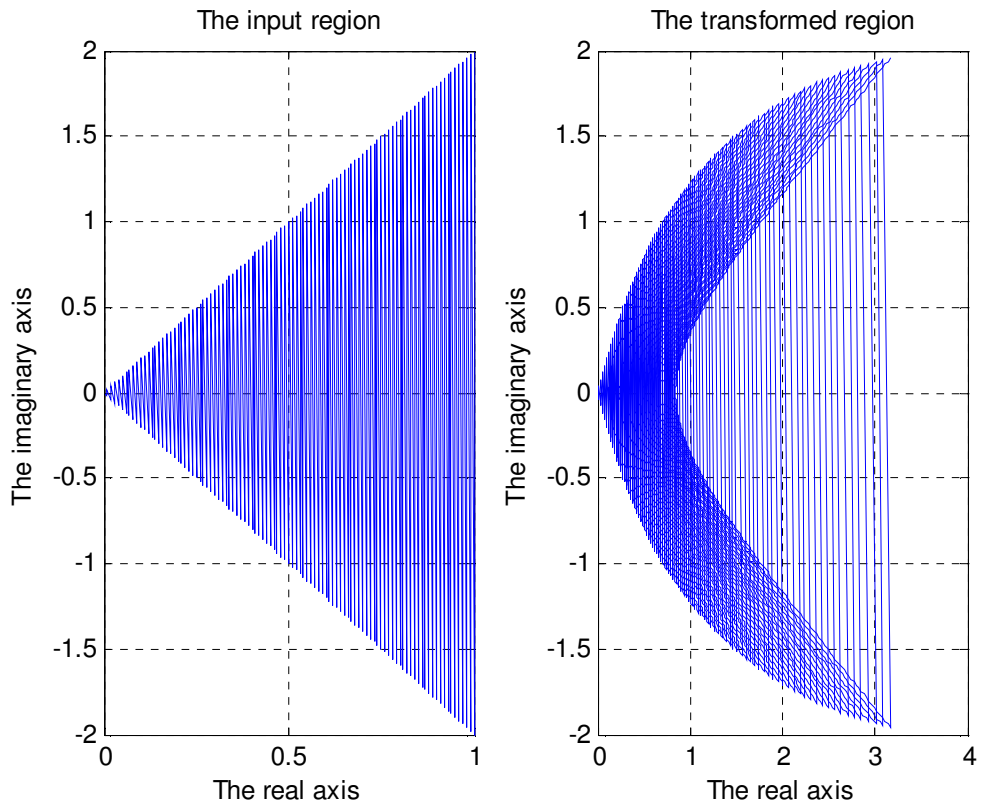


Figure 2. $w = \sin(z)$