

Reducing Anchor Loss in Micromechanical Extensional Mode Resonators

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Abstract—In this work, we propose a novel method to increase the quality factor of extensional mode micromechanical resonators. The proposed resonator topology is suitable for integration in a silicon-based process to fabricate micromechanical filters and oscillators. It is a half-wavelength-long strip excited longitudinally by electrostatic forces, and it is isolated from the substrate by alternating with bars of a quarter wavelength long. This structure causes a large impedance mismatch between the resonator and the substrate and hence reduces the anchor loss considerably. The performance of the resonator is determined by finite element simulations. We introduce an equivalent electrical circuit to predict the performance of the resonator. The electrical model gives results consistent with the finite element simulations. The proposed resonator is expected to have a very small anchor loss resulting in a very high Q .

I. INTRODUCTION

MICROMECHANICAL filters have been fabricated by integrated circuit compatible techniques [1], which showed their potential to replace off-chip surface acoustic wave or crystal filter counterparts. To have high frequency selectivity, the resonators of the filter should have high quality factors on the order of 10,000 [2] to be used in radio frequency applications. The energy dissipation mechanisms that determine the quality factor in micromachined structures are air damping, anchor loss, thermoelastic dissipation, surface loss, and internal (material) dissipation [3]. Bulk mode extensional resonators have reached very high quality factors [4]. Their stiffness, in the order of 10^6 N/m, enables such resonators to store a high amount of energy. With this characteristic, in contrast to the flexural resonators, bulk extensional resonators can achieve very high Q values with the same amount of air damping per cycle [1], [5].

At high frequencies, the main loss mechanism that determines the Q value in extensional mode resonators is the anchor loss [6]. Several designs have been implemented to eliminate the anchor loss in micromachined structures. Resonators have been anchored to the substrate at their nodal points [1], [7] to reduce the energy coupled to the substrate. Techniques based on impedance mismatch have

been used in several designs. Newell suggested using Bragg reflectors composed of different material types [8]. Wang *et al.* have implemented material mismatched disk resonators [9]. Impedance mismatch between the polysilicon and the diamond reduced anchor loss considerably, and a Q value of 11555 was obtained at 1.5 GHz. The reflection property of the quarter-wavelength beams was used to reduce support loss in [10]. In another work, thinner beams were used to attach bulk micromachined resonators to the substrate [11].

In this paper, we introduce a new isolation mechanism to eliminate anchor loss. We use quarter-wavelength long strips with alternating low and high impedances to transform the impedance of the substrate to a very small value. Hence, the anchor of the resonator is connected to a very low impedance, and very little energy coupling occurs. Because the impedance of a strip is proportional to the cross-sectional area of the strip, we use alternating width strips with the same thickness to decouple the resonator from the substrate. No other material type is required, and the fabrication process is relatively simple. In what follows, we will explain a reflection mechanism in mechanical bars. Based on this mechanism, we will introduce a novel method to connect the resonator to the substrate to reduce the anchor loss. An electrical equivalent circuit will be presented to predict the behavior of the resonator without finite element simulations. Finally, simulation results will be presented showing the performance of the resonator.

II. ANALOGOUS ELECTRICAL CIRCUIT

Let us first investigate the acoustic wave propagation in a thin rod. There may be several modes present in a thin rod depending on the frequency of excitation. In rectangular rods, the zeroth-order longitudinal mode propagation is nondispersive [12]. Higher and dispersive modes are excited above a certain frequency. Below this frequency, all dispersive modes are evanescent. If the length of the rod, L , is much greater than its width, W , and its thickness, T ($T < W$), the closest higher order plate mode resonance occurs at $f_1 = f_o \sqrt{1 + (L/W)^2}$ [12] where f_o is the frequency at which L equals $\lambda/2$. If L/W is sufficiently large, f_1 is far away. In this work, we assume an operation below f_1 and approximate 3-D waves in the rod with 1-D zeroth order longitudinal (extensional) waves. Finite element simulations (ANSYS, Inc., Canonsburg, PA; see Fig. 1) of rods with modest L/W ratios show that the waves in the rods are not strictly longitudinal. Nevertheless, the approximation gets better as the L/W ratio is made higher.

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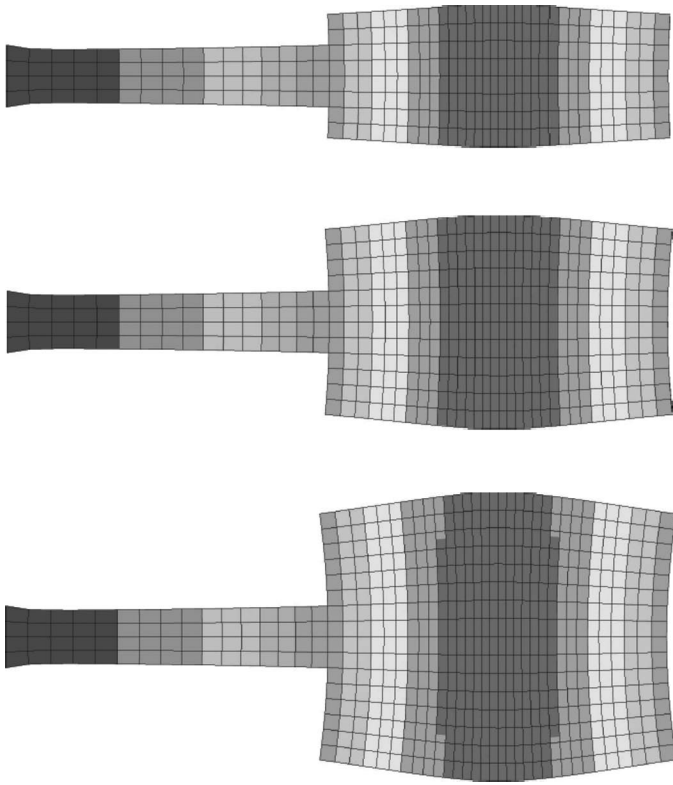


Fig. 1. Finite element simulations showing the standing waves in rods of different L/W ratios.

Nondispersive wave propagation in these mechanical rods are analogous to wave propagation in electrical transmission lines.¹ Counterparts of force and particle velocity in the mechanical domain are voltage and current in the electrical domain, respectively. Hence, the characteristic impedance (Z) of a transmission line is the analog of the mechanical characteristic impedance of a rod. Z of a rod for the zeroth-order nondispersive mode can be written as a frequency independent parameter [13]

$$Z = A \frac{E}{c} = A \sqrt{E\rho}, \quad (1)$$

where $A = WT$ is the cross-sectional area of the rod, E is the Young's modulus, ρ is the density of the rod, and c is the phase velocity of the extensional mode with $c = \sqrt{E/\rho}$. Z has the unit of kilograms per second. Fig. 2 illustrates an infinitely long rod connected to another rod of the same thickness but of a smaller width. A_1 and A_2 represent the respective cross-sectional areas of the rods. When an extensional mode stress wave is incident from the first rod to the second rod, the stress wave is reflected with a reflection coefficient of R and is transmitted to the second region with a transmission coefficient of T :

$$R = \frac{Z_2 - Z_1}{Z_1 + Z_2} \quad T = \frac{2Z_2}{Z_1 + Z_2}, \quad (2)$$

¹Because the electrical transmission lines are nondispersive, it is not possible to represent dispersive acoustic modes with a transmission line analogy.

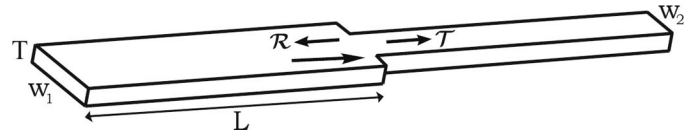


Fig. 2. Incident, reflected (R) and transmitted (T) stress waves at a discontinuity in an acoustic bar of uniform thickness, T .

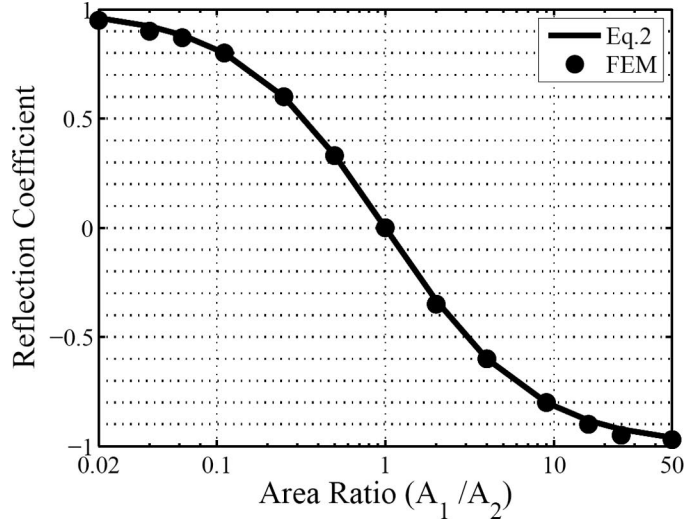


Fig. 3. Calculated (solid line) and simulated (dots) reflection coefficient of stress wave as a function of area ratio.

where Z_1 and Z_2 represent the respective mechanical characteristic impedances of the rods. It is clear from this equation that $Z_1/Z_2 = A_1/A_2$ must be made as away as possible from 1 to minimize the transmitted power. A transient analysis was done to examine the validity of (2) using the finite element package. Fig. 3 shows the reflection coefficient of stress waves along the axis of the rod from finite element simulations in comparison to that from (2) for various A_1/A_2 values. We can see that the first order approximation of (1) is valid in a wide range $0.02 < Z_1/Z_2 < 50$.

The rods are typically connected to a substrate at one end to form a resonator. If the substrate is sufficiently large, any energy coupled to the substrate can be considered to be lost. Hence, the substrate connection can be modeled as a resistance in the analogous electrical circuit. To complete the picture, we need to express the value of this resistance in the mechanical domain.

Suppose that the attachment point vibrates in response to uniform axial stress of σ_x at the clamped end. The corresponding force at the attachment is $\sigma_x A$. To calculate the displacement of the attachment, Hao *et al.* [14], [15] model the support as an infinite elastic medium. For a circular² cross section of area A , the displacement of the attachment point is given by [14]

²A rectangular cross section with the same area should give the same results as long as the cross-sectional dimensions are much smaller than the wavelength. However, this statement is inconsistent with the results in [14]. Comparison of 3-D FEM simulations with circular and rectangular cross sections showed that the results are within 2% of each other, rather than the 2π ratio existing between (37) and (46) of [14].

$$u_x = \frac{\sigma_x A \omega \gamma F(\gamma)}{2\pi \rho c_t^3}, \quad (3)$$

with

$$c_t = \sqrt{\frac{E}{2\rho(1+\nu)}}, \quad (4)$$

$$\gamma = \sqrt{\frac{2(1-\nu)}{1-2\nu}}, \quad (5)$$

where ν is the Poisson ratio of the rod material and w is the angular excitation frequency. $F(\gamma)$ is given by the imaginary part of an integral [14]:

$$F(\gamma) = \text{Im} \int_0^\infty \frac{\kappa \zeta}{(\gamma^2 - 2\zeta^2)^2 - 4\kappa \zeta^2 \sqrt{\zeta^2 - \gamma^2}} d\zeta, \quad (6)$$

with $\kappa = \sqrt{\zeta^2 - 1}$.

At this point we can define the equivalent resistance, R , representing the energy lost into the substrate. Its value can be found by dividing the force, $\sigma_x A$, by the particle velocity, ωu_x :

$$R = \frac{2\pi c_t^3 \rho}{\gamma F(\gamma)} \frac{1}{\omega^2} = \frac{4}{\pi} \rho K c \lambda^2, \quad (7)$$

where

$$K = \frac{1}{16\sqrt{2}\gamma F(\gamma)(1+\nu)^{3/2}}. \quad (8)$$

The unit for R is kilograms per second, and it is consistent with the unit of Z . It is clear that R can be made large by choosing a high stiffness, low-density material. We note that the quantities Z/A and R/λ^2 are dependent only on the material constants. Values of K , Z/A , and R/λ^2 for several materials are listed in Table I.

III. MECHANICAL QUALITY FACTOR OF SUSPENDED RESONATORS

A. Quarter-Wavelength Resonator

First, let us consider a quarter-wavelength long, $L = c/(4f) = \lambda/4$, resonator connected to a substrate at one end as shown in Fig. 4. The analogous electrical circuit is depicted in the same figure. The resonator and its substrate connection are modeled by an electrical transmission line

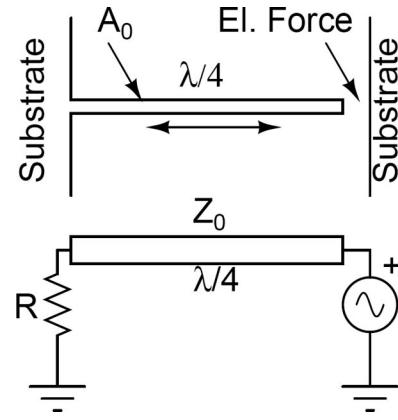


Fig. 4. A $\lambda/4$ mechanical resonator with a cross-sectional area of A_0 and its electrical equivalent circuit.

and a resistor, respectively. To get a high quality factor, the condition $R \gg Z_0$ is imposed. The electrostatic excitation force of the mechanical resonator is represented by a voltage source in the electrical equivalent. To determine the quality factor of this circuit, the impedance seen by the voltage source is written from the transmission line equation [16] as

$$Z_{in0} = Z_0 \frac{R + jZ_0 \tan(\pi f/2f_0)}{Z_0 + jR \tan(\pi f/2f_0)}, \quad (9)$$

where f is the operation frequency and f_0 is the frequency at which the transmission line is a quarter wavelength. If f is close to f_0 , $\tan(\pi f/2f_0) \approx 2f_0/(\pi(f_0 - f))$ and it is very large. Using this approximation and ignoring the real part of the denominator, (9) becomes

$$Z_{in0} \approx Z_0 \frac{R + jZ_0 2f_0/(\pi(f_0 - f))}{jR 2f_0/(\pi(f_0 - f))} = \frac{Z_0^2}{R} - j\frac{\pi}{2} Z_0 \frac{f_0 - f}{f_0}. \quad (10)$$

At 3-dB frequencies (f_1 and f_2), the real part of Z_{in} will be equal to the absolute value of the imaginary part:

$$\frac{Z_0^2}{R} = \frac{\pi}{2} Z_0 \frac{f_0 - f_1}{f_0} = \frac{\pi}{2} Z_0 \frac{f_2 - f_0}{f_0}. \quad (11)$$

The quality factor, Q_0 , is the center frequency divided by the 3-dB bandwidth:

$$Q_0 = \frac{f_0}{f_2 - f_1} = \frac{\pi}{4} \frac{R}{Z_0}. \quad (12)$$

TABLE I. VALUES OF CONSTANTS FOR DIFFERENT MATERIALS.

Material	K	Z/A (kg/m ² /s)	R/λ^2 (kg/m ² /s)
Silicon Oxide	0.112	$1.24 \cdot 10^7$	$1.77 \cdot 10^6$
Silicon	0.101	$1.86 \cdot 10^7$	$2.41 \cdot 10^6$
Polysilicon	0.107	$1.92 \cdot 10^7$	$2.62 \cdot 10^6$
Silicon Nitride	0.106	$2.78 \cdot 10^7$	$3.75 \cdot 10^6$
Polydiamond	0.118	$6.20 \cdot 10^7$	$9.33 \cdot 10^6$

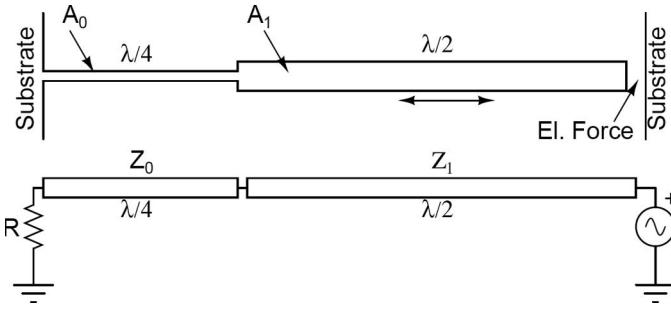


Fig. 5. A $\lambda/2$ resonator supported with a $\lambda/4$ bar and its electrical equivalent circuit.

Hence, the quality factor of the mechanical resonator due to anchor loss can be deduced by combining (1), (7), and (12):

$$Q_0 = K \frac{\lambda^2}{A_0}. \quad (13)$$

It is clear that a high value of λ^2/A_0 will result in a better quality factor. The resonator should have as small cross section as possible.

B. Half-Wavelength Resonator

In this case, $L = c/(2f) = \lambda/2$. The quality factor of the resonator from the electrical circuit can be deduced using a derivation similar to that given above:

$$Q = \frac{\pi}{2} \frac{Z_1}{R}. \quad (14)$$

From (1) and (7) we find

$$Q = \frac{\pi^2}{8K} \frac{A_1}{\lambda^2}. \quad (15)$$

In this case, A_1/λ^2 must be large to have a high quality factor resonator. However, this requirement contradicts with the requirement that the length of the resonator should be much longer than its width to guarantee zeroth-mode operation. We conclude that a half-wavelength rod connected to a substrate directly does not result in a high Q resonator.

C. Half-Wavelength Resonator Supported with a Quarter-Wavelength Bar

A half-wavelength resonator is connected to the substrate through a quarter-wavelength bar with $A_1 > A_0$ as illustrated in Fig. 5. The electrical equivalent circuit can be analyzed to determine the quality factor. The impedance, Z_{in1} , seen by the voltage source is

$$Z_{in1} = Z_1 \frac{Z_{in0} + jZ_1 \tan(\pi f/f_0)}{Z_1 + jZ_{in0} \tan(\pi f/f_0)}. \quad (16)$$

The imaginary part in the denominator can be ignored when f is near f_0 , because $Z_1 \gg Z_{in0}$. Substituting (10) in (16) and using $\tan(\pi f/f_0) \approx \pi(f - f_0)/f_0$ we find

$$Z_{in1} = \frac{Z_0^2}{R} - j\frac{\pi}{2} Z_0 \frac{f_0 - f}{f_0} + j\pi Z_1 \frac{f - f_0}{f_0}. \quad (17)$$

Equating the real part to the imaginary part to find the 3-dB frequencies

$$\frac{Z_0^2}{R} = \left(\frac{\pi}{2} Z_0 + \pi Z_1 \right) \frac{f_0 - f_1}{f_0} = \left(\frac{\pi}{2} Z_0 + \pi Z_1 \right) \frac{f_2 - f_0}{f_0}. \quad (18)$$

Hence, Q of this circuit is given by

$$Q_1 = \frac{\pi}{4} \frac{R}{Z_0} \left(1 + \frac{2Z_1}{Z_0} \right). \quad (19)$$

Using (1) and (7) we find

$$Q_1 = K \frac{\lambda^2}{A_0} (1 + 2r), \quad (20)$$

with $r = A_1/A_0$. Clearly, the quality factor improves with $(1 + 2r)$. Making the area ratio r as large as possible will result in a high Q resonator.

D. Half-Wavelength Resonator Supported with 3 Quarter-Wavelength Sections

We can add 2 more quarter-wavelength sections to improve the quality factor even more as shown in Fig. 6. The half-wavelength resonator is connected to the substrate through 3 quarter-wavelength sections. From the electrical circuit of this combination we find

$$Q_2 = \frac{\pi}{4} \frac{R}{Z_0} \left(1 + \frac{Z_1}{Z_0} + \left(\frac{Z_2}{Z_0} + \frac{2Z_3}{Z_0} \right) \left(\frac{Z_1}{Z_2} \right)^2 \right). \quad (21)$$

Using (1) and (7), we find

$$Q_2 = K \frac{\lambda^2}{A_0} \left(1 + \frac{A_1}{A_0} + \left(\frac{A_2}{A_0} + \frac{2A_3}{A_0} \right) \left(\frac{A_1}{A_2} \right)^2 \right). \quad (22)$$

This equation shows that the area ratio between neighboring elements must be large to generate a high-quality system. For the special case of $r = A_1/A_0 = A_3/A_2$ with $A_0 = A_2$, we find

$$Q_2 = K \frac{\lambda^2}{A_0} (1 + r + r^2 + 2r^3). \quad (23)$$

With a modest area ratio of $r = 5$, the improvement in the quality factor is 281. Harmonic analysis was done in the FEM simulator to observe the amount of stress at the clamped region. The stress at the anchor point is mini-

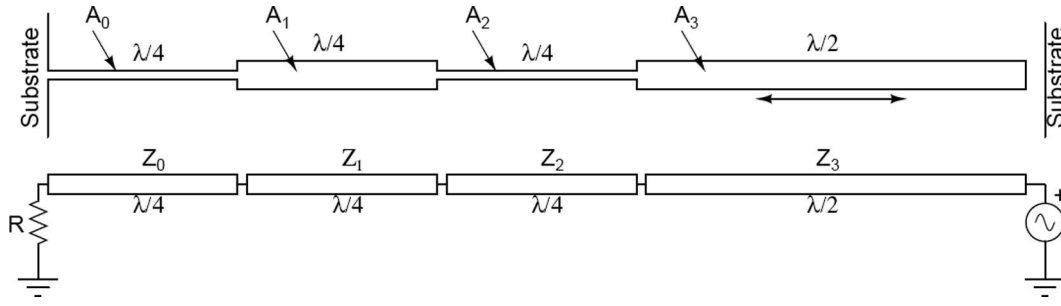


Fig. 6. A half-wave resonator supported with 3 quarter-wave sections and its equivalent circuit.

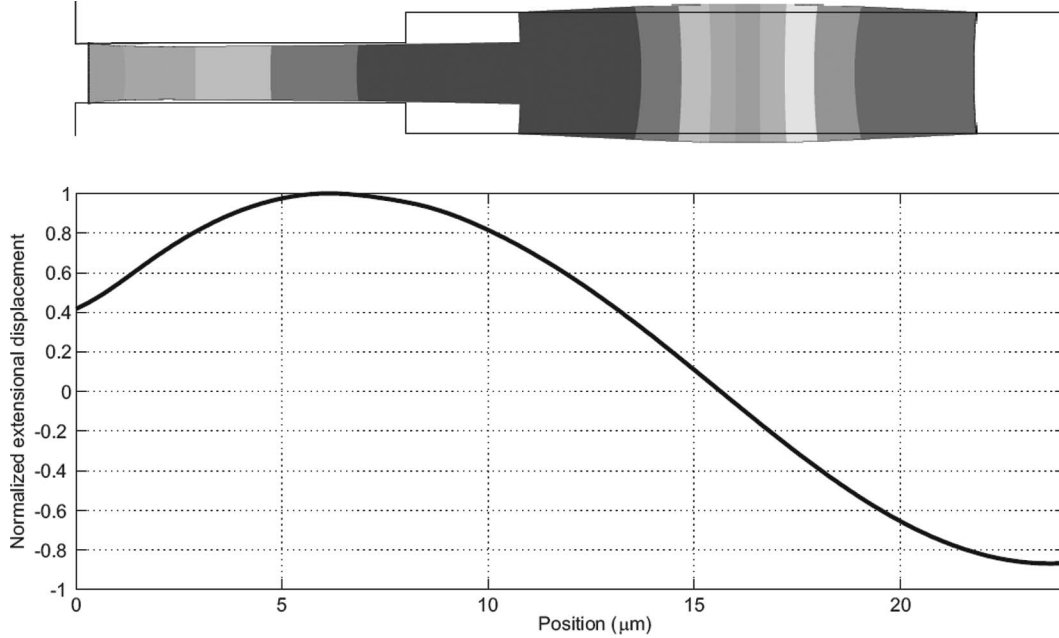


Fig. 7. Deformed and undeformed shapes of the $\lambda/2$ resonator supported by a $\lambda/4$ section as found from FEM. Lower figure is the displacement amplitude along the axis of the bars.

mized by successful operation of the quarter-wavelength sections.

E. Half-Wavelength Resonator Supported with an Odd Number of Quarter-Wavelength Sections

We can generalize the formula of (23) to n pair of resonators as follows:

$$Q_n = K \frac{\lambda^2}{A_0} (1 + r + r^2 + \dots + r^{2n-2} + 2r^{2n-1}). \quad (24)$$

F. Odd-Overtone Resonances

The structures above resonate also at an odd multiple of the fundamental frequency. The corresponding quality factor at those frequencies can be determined easily from the electrical equivalent circuit. If the overtone resonance is at $(2m + 1)$ multiple, the quality factors of electrical equivalent circuits as given by (12), (19), and (21) predict a quality factor improvement of $(2m + 1)$. However, the

anchor loss represented by R is proportional to λ^2 , and hence R decreases by the factor $(2m + 1)^2$ at these odd-overtones. We conclude that in all the structures above the quality factor at the $(2m + 1)$ th resonance is reduced by a factor of $1/(2m + 1)$. So, using overtone resonances is not advantageous. For example, the resonator of Fig. 5 ($3\lambda/4$ long) is better than a uniform 3-quarter-wavelength (third-overtone) resonator.

IV. SIMULATION RESULTS

We have verified the validity of (13), (20), and (23) by a finite element simulator. We used COMSOL (COMSOL, Inc., Burlington, MA) because it can handle a propagation into a semi-infinite medium very well. Perfectly matched layers (PML), which are constructed by complex coordinate transformation, have been implemented to find anchor loss [17]. In the FEM package, PML domains are available for several analysis types. We worked with resonators with circular cross sections rather than rectangular to get axially symmetric structures for a better accuracy.

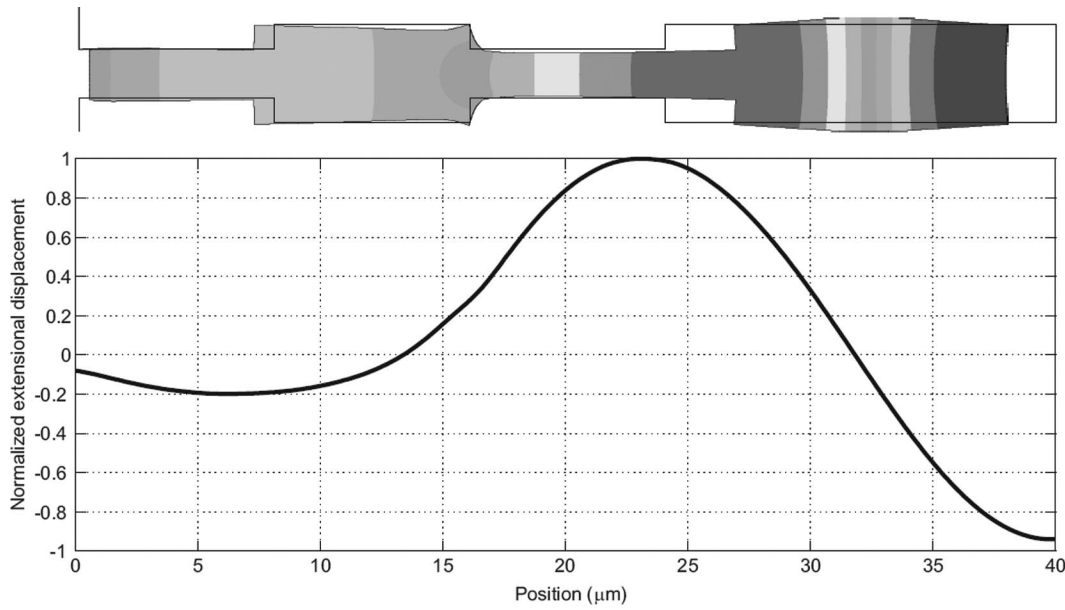


Fig. 8. Deformed and undeformed shapes of the $\lambda/2$ resonator supported by 3 $\lambda/4$ sections as found from FEM. Lower figure is the displacement amplitude along the axis of the bars.

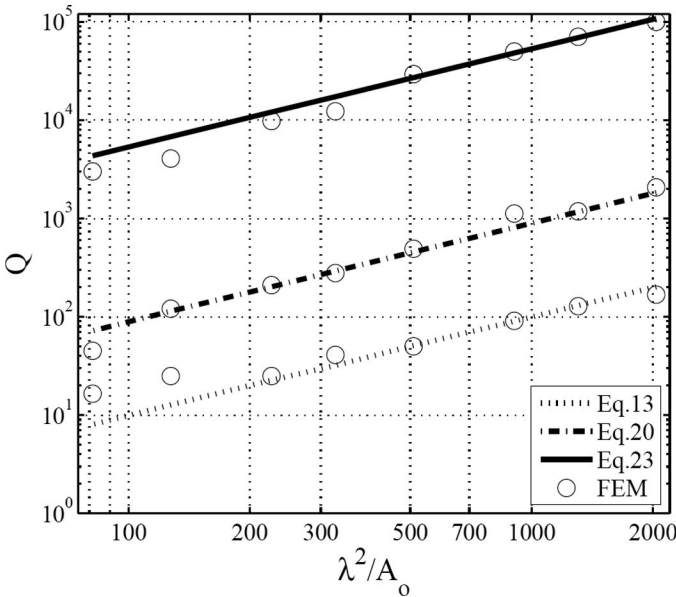


Fig. 9. A comparison of finite element simulation results with the analytical formula: Q of silicon resonators for varying λ^2/A_0 ratios. Q_0 of a quarter-wave resonator (lower curve), Q_1 of half-wave resonator with one $\lambda/4$ support with $r = 4$ (middle curve), and Q_2 of half-wave resonator with 3 $\lambda/4$ supports with $r = 6.25$ (upper curve). $E = 150$ GPa, $\rho = 2330$ kg/m³, and $\nu = 0.3$ have been used for the silicon material properties.

We applied a uniform force parallel to the axis of the resonator at the free end to simulate the typical electrostatic excitation. Fig. 7 illustrates the deformed and undeformed shapes of a $\lambda/2$ -long 250-MHz resonator supported by a $\lambda/4$ section. The same figure also has a plot of the displacement amplitude along the resonator. Fig. 8 contains similar figures for the same resonator supported by 3 quarter-wave sections. Clearly, the displacement amplitude at the anchor gets smaller with more support sections.

We performed frequency response analysis to extract the quality factor. Fig. 9 is a comparison of Q values due to anchor loss, as obtained from the analytical expressions and the finite element simulation results. The quality factor of a silicon quarter-wave resonator at 250 MHz is plotted in the lower curve. For the half-wavelength resonator supported by a quarter-wavelength bar we chose $r = 4$. Eq. (20) is plotted along with finite element simulation results in the middle of Fig. 9. In the same figure, a half-wavelength resonator with 3 quarter-wave support rods is also shown. We chose $A_0 = A_2$, $A_1/A_0 = 6.25$, and $A_1 = A_3$ ($r = 6.25$). Differences between the curves and FEM results can be attributed to the errors in simulations and deviations from the transmission line approximations as λ^2/A_0 ratio decreases.

The proposed resonant structures can be fabricated using a variety of available micromachining processes including [1] and [7]. A typical silicon half-wavelength resonator at 250 MHz should be 16- μ m long and several microns wide.

V. CONCLUSIONS

A new method has been proposed to reduce anchor losses in micromachined structures. The method is superior to other isolation methods in terms of ease in the fabrication processes. An electrical equivalent circuit is introduced with a resistance modeling the anchor loss. Equations predicting the quality factors of extensional resonator with different support structures are derived. The formulas are optimistic because they include only the anchor loss. The FEM simulation results are consistent with the predictions. The proposed resonator structure is

a promising high-Q building block in RF micromechanical filters and oscillators.

ACKNOWLEDGMENTS

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